

# Mathematica 11.3 Integration Test Results

Test results for the 96 problems in "1.2.3.3 (d+e x^n)^q (a+b x^n+c x^(2 n))^p.m"

Problem 5: Result is not expressed in closed-form.

$$\int \frac{d + e x^4}{d^2 + b x^4 + e^2 x^8} dx$$

Optimal (type 3, 791 leaves, 19 steps):

$$\begin{aligned} & \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}-2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}-2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}} + \\ & \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}+2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}+2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}} - \\ & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}} + \\ & \frac{\text{Log}\left[\sqrt{d}+\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{-b+2de}} - \\ & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}} + \frac{\text{Log}\left[\sqrt{d}+\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{-b+2de}} \end{aligned}$$

Result (type 7, 67 leaves):

$$\frac{1}{4} \text{RootSum}\left[d^2 + b \#1^4 + e^2 \#1^8 \&, \frac{d \text{Log}[x - \#1] + e \text{Log}[x - \#1] \#1^4}{b \#1^3 + 2 e^2 \#1^7} \&\right]$$

Problem 6: Result is not expressed in closed-form.

$$\int \frac{d + e x^4}{d^2 + f x^4 + e^2 x^8} dx$$

Optimal (type 3, 791 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}-2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}-2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}} + \\
 & \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}+2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}+2\sqrt{e}x}{\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}}\right]}{4\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}} - \\
 & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}} + \frac{\text{Log}\left[\sqrt{d}+\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}-\sqrt{2de-f}} - \\
 & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}} + \frac{\text{Log}\left[\sqrt{d}+\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2}\sqrt{d}\sqrt{e}+\sqrt{2de-f}}
 \end{aligned}$$

Result (type 7, 67 leaves):

$$\frac{1}{4} \text{RootSum}\left[d^2 + f \#1^4 + e^2 \#1^8 \&, \frac{d \text{Log}[x - \#1] + e \text{Log}[x - \#1] \#1^4}{f \#1^3 + 2 e^2 \#1^7} \&\right]$$

Problem 7: Result is not expressed in closed-form.

$$\int \frac{d + e x^4}{d^2 - b x^4 + e^2 x^8} dx$$

Optimal (type 3, 349 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{\sqrt{e} \text{ArcTan}\left[\frac{\sqrt{2}\sqrt{e}x}{\sqrt{\sqrt{b-2de}-\sqrt{b+2de}}}\right]}{\sqrt{2}\sqrt{b-2de}\sqrt{\sqrt{b-2de}-\sqrt{b+2de}}} - \frac{\sqrt{e} \text{ArcTan}\left[\frac{\sqrt{2}\sqrt{e}x}{\sqrt{\sqrt{b-2de}+\sqrt{b+2de}}}\right]}{\sqrt{2}\sqrt{b-2de}\sqrt{\sqrt{b-2de}+\sqrt{b+2de}}} - \\
 & \frac{\sqrt{e} \text{ArcTanh}\left[\frac{\sqrt{2}\sqrt{e}x}{\sqrt{\sqrt{b-2de}-\sqrt{b+2de}}}\right]}{\sqrt{2}\sqrt{b-2de}\sqrt{\sqrt{b-2de}-\sqrt{b+2de}}} - \frac{\sqrt{e} \text{ArcTanh}\left[\frac{\sqrt{2}\sqrt{e}x}{\sqrt{\sqrt{b-2de}+\sqrt{b+2de}}}\right]}{\sqrt{2}\sqrt{b-2de}\sqrt{\sqrt{b-2de}+\sqrt{b+2de}}}
 \end{aligned}$$

Result (type 7, 69 leaves):

$$\frac{1}{4} \text{RootSum}\left[d^2 - b \#1^4 + e^2 \#1^8 \&, \frac{d \text{Log}[x - \#1] + e \text{Log}[x - \#1] \#1^4}{-b \#1^3 + 2 e^2 \#1^7} \&\right]$$

Problem 8: Result is not expressed in closed-form.

$$\int \frac{d + e x^4}{d^2 - f x^4 + e^2 x^8} dx$$

Optimal (type 3, 751 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{\text{ArcTan}\left[\frac{\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}-2\sqrt{e}x}{\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}\right]}{4\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}-\frac{\text{ArcTan}\left[\frac{\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}-2\sqrt{e}x}{\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}\right]}{4\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}+ \\
 & \frac{\text{ArcTan}\left[\frac{\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}+2\sqrt{e}x}{\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}\right]}{4\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}+\frac{\text{ArcTan}\left[\frac{\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}+2\sqrt{e}x}{\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}\right]}{4\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}- \\
 & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}+\frac{\text{Log}\left[\sqrt{d}+\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}-\sqrt{2de+f}}}- \\
 & \frac{\text{Log}\left[\sqrt{d}-\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}+\frac{\text{Log}\left[\sqrt{d}+\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}x+\sqrt{e}x^2\right]}{8\sqrt{d}\sqrt{2\sqrt{d}\sqrt{e}+\sqrt{2de+f}}}
 \end{aligned}$$

Result (type 7, 69 leaves):

$$\frac{1}{4}\text{RootSum}\left[d^2-f\#1^4+e^2\#1^8\&, \frac{d\text{Log}[x-\#1]+e\text{Log}[x-\#1]\#1^4}{-f\#1^3+2e^2\#1^7}\&\right]$$

Problem 9: Result is not expressed in closed-form.

$$\int \frac{1+x^4}{1+bx^4+x^8} dx$$

Optimal (type 3, 411 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{2-b}}-2x}{\sqrt{2+\sqrt{2-b}}}\right]}{4\sqrt{2+\sqrt{2-b}}}-\frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{2-b}}-2x}{\sqrt{2-\sqrt{2-b}}}\right]}{4\sqrt{2-\sqrt{2-b}}}+\frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{2-b}}+2x}{\sqrt{2+\sqrt{2-b}}}\right]}{4\sqrt{2+\sqrt{2-b}}}+ \\
 & \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{2-b}}+2x}{\sqrt{2-\sqrt{2-b}}}\right]}{4\sqrt{2-\sqrt{2-b}}}-\frac{\text{Log}\left[1-\sqrt{2-\sqrt{2-b}}x+x^2\right]}{8\sqrt{2-\sqrt{2-b}}}+\frac{\text{Log}\left[1+\sqrt{2-\sqrt{2-b}}x+x^2\right]}{8\sqrt{2-\sqrt{2-b}}}- \\
 & \frac{\text{Log}\left[1-\sqrt{2+\sqrt{2-b}}x+x^2\right]}{8\sqrt{2+\sqrt{2-b}}}+\frac{\text{Log}\left[1+\sqrt{2+\sqrt{2-b}}x+x^2\right]}{8\sqrt{2+\sqrt{2-b}}}
 \end{aligned}$$

Result (type 7, 55 leaves):

$$\frac{1}{4}\text{RootSum}\left[1+b\#1^4+\#1^8\&, \frac{\text{Log}[x-\#1]+\text{Log}[x-\#1]\#1^4}{b\#1^3+2\#1^7}\&\right]$$

Problem 10: Result is not expressed in closed-form.

$$\int \frac{1+x^4}{1+3x^4+x^8} dx$$

Optimal (type 3, 451 leaves, 19 steps):

$$\begin{aligned} & -\frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1-\frac{2^{3/4} x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} + \frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1+\frac{2^{3/4} x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} \\ & -\frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1-\frac{2^{3/4} x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} + \frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1+\frac{2^{3/4} x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4} \sqrt{5}} \\ & +\frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})}-2(2(3-\sqrt{5}))^{1/4} x+2 x^2\right]}{4 \times 2^{3/4} \sqrt{5}} \\ & -\frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})}+2(2(3-\sqrt{5}))^{1/4} x+2 x^2\right]}{4 \times 2^{3/4} \sqrt{5}} \\ & +\frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})}-2(2(3+\sqrt{5}))^{1/4} x+2 x^2\right]}{4 \times 2^{3/4} \sqrt{5}} \\ & +\frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})}+2(2(3+\sqrt{5}))^{1/4} x+2 x^2\right]}{4 \times 2^{3/4} \sqrt{5}} \end{aligned}$$

Result (type 7, 55 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1+3 \#1^4+\#1^8, \frac{\operatorname{Log}[x-\#1]+\operatorname{Log}[x-\#1] \#1^4}{3 \#1^3+2 \#1^7} \& \right]$$

**Problem 12: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{1+x^4}{1+x^4+x^8} dx$$

Optimal (type 3, 140 leaves, 19 steps):

$$\begin{aligned} & -\frac{\operatorname{ArcTan}\left[\frac{1-2 x}{\sqrt{3}}\right]}{4 \sqrt{3}} - \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}-2 x] + \frac{\operatorname{ArcTan}\left[\frac{1+2 x}{\sqrt{3}}\right]}{4 \sqrt{3}} + \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}+2 x] - \\ & \frac{1}{8} \operatorname{Log}[1-x+x^2] + \frac{1}{8} \operatorname{Log}[1+x+x^2] - \frac{\operatorname{Log}[1-\sqrt{3} x+x^2]}{8 \sqrt{3}} + \frac{\operatorname{Log}[1+\sqrt{3} x+x^2]}{8 \sqrt{3}} \end{aligned}$$

Result (type 3, 135 leaves):

$$\frac{1}{48} \left( 4 i \sqrt{-6-6 i \sqrt{3}} \operatorname{ArcTan}\left[\frac{1}{2}(1-i \sqrt{3}) x\right]-4 i \sqrt{-6+6 i \sqrt{3}} \operatorname{ArcTan}\left[\frac{1}{2}(1+i \sqrt{3}) x\right]+4 \sqrt{3} \operatorname{ArcTan}\left[\frac{-1+2 x}{\sqrt{3}}\right]+4 \sqrt{3} \operatorname{ArcTan}\left[\frac{1+2 x}{\sqrt{3}}\right]-6 \operatorname{Log}\left[1-x+x^2\right]+6 \operatorname{Log}\left[1+x+x^2\right] \right)$$

**Problem 14: Result is not expressed in closed-form.**

$$\int \frac{1+x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 331 leaves, 19 steps):

$$\begin{aligned} & -\frac{1}{4} \sqrt{2-\sqrt{3}} \operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2 x}{\sqrt{2+\sqrt{3}}}\right]- \\ & \frac{1}{4} \sqrt{2+\sqrt{3}} \operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2 x}{\sqrt{2-\sqrt{3}}}\right]+\frac{1}{4} \sqrt{2-\sqrt{3}} \operatorname{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2 x}{\sqrt{2+\sqrt{3}}}\right]+ \\ & \frac{1}{4} \sqrt{2+\sqrt{3}} \operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2 x}{\sqrt{2-\sqrt{3}}}\right]-\frac{\operatorname{Log}\left[1-\sqrt{2-\sqrt{3}} x+x^2\right]}{8 \sqrt{2-\sqrt{3}}}+ \\ & \frac{\operatorname{Log}\left[1+\sqrt{2-\sqrt{3}} x+x^2\right]}{8 \sqrt{2-\sqrt{3}}}-\frac{\operatorname{Log}\left[1-\sqrt{2+\sqrt{3}} x+x^2\right]}{8 \sqrt{2+\sqrt{3}}}+\frac{\operatorname{Log}\left[1+\sqrt{2+\sqrt{3}} x+x^2\right]}{8 \sqrt{2+\sqrt{3}}} \end{aligned}$$

Result (type 7, 55 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{\operatorname{Log}\left[x-\#1\right]+\operatorname{Log}\left[x-\#1\right] \#1^4}{-\#1^3+2 \#1^7} \&\right]$$

**Problem 17: Result is not expressed in closed-form.**

$$\int \frac{1+x^4}{1-4 x^4+x^8} dx$$

Optimal (type 3, 157 leaves, 7 steps):

$$\frac{\operatorname{ArcTan}\left[\frac{2^{1/4} x}{\sqrt{-1+\sqrt{3}}}\right]}{2 \times 2^{1/4} \sqrt{-1+\sqrt{3}}}-\frac{\operatorname{ArcTan}\left[\frac{2^{1/4} x}{\sqrt{1+\sqrt{3}}}\right]}{2 \times 2^{1/4} \sqrt{1+\sqrt{3}}}+\frac{\operatorname{ArcTanh}\left[\frac{2^{1/4} x}{\sqrt{-1+\sqrt{3}}}\right]}{2 \times 2^{1/4} \sqrt{-1+\sqrt{3}}}-\frac{\operatorname{ArcTanh}\left[\frac{2^{1/4} x}{\sqrt{1+\sqrt{3}}}\right]}{2 \times 2^{1/4} \sqrt{1+\sqrt{3}}}$$

Result (type 7, 53 leaves):

$$\frac{1}{8} \operatorname{RootSum}\left[1-4 \#1^4+\#1^8 \&, \frac{\operatorname{Log}\left[x-\#1\right]+\operatorname{Log}\left[x-\#1\right] \#1^4}{-2 \#1^3+\#1^7} \&\right]$$

**Problem 18: Result is not expressed in closed-form.**

$$\int \frac{1+x^4}{1-5x^4+x^8} dx$$

Optimal (type 3, 171 leaves, 7 steps):

$$\frac{\text{ArcTan}\left[\sqrt{\frac{2}{-\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{6(-\sqrt{3}+\sqrt{7})}} - \frac{\text{ArcTan}\left[\sqrt{\frac{2}{\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{6(\sqrt{3}+\sqrt{7})}} + \frac{\text{ArcTanh}\left[\sqrt{\frac{2}{-\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{6(-\sqrt{3}+\sqrt{7})}} - \frac{\text{ArcTanh}\left[\sqrt{\frac{2}{\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{6(\sqrt{3}+\sqrt{7})}}$$

Result (type 7, 55 leaves):

$$\frac{1}{4} \text{RootSum}\left[1-5 \#1^4+\#1^8 \&, \frac{\text{Log}[x-\#1]+\text{Log}[x-\#1] \#1^4}{-5 \#1^3+2 \#1^7} \&\right]$$

**Problem 20: Result is not expressed in closed-form.**

$$\int \frac{1-x^4}{1+bx^4+x^8} dx$$

Optimal (type 3, 511 leaves, 19 steps):

$$\begin{aligned} & -\frac{\sqrt{2+b} \text{ArcTan}\left[\frac{\sqrt{2-\sqrt{2-b}}-2x}{\sqrt{2+\sqrt{2-b}}}\right]}{4\sqrt{2-\sqrt{2-b}}\sqrt{2-b}} + \frac{\sqrt{2+b} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{2-b}}-2x}{\sqrt{2-\sqrt{2-b}}}\right]}{4\sqrt{2+\sqrt{2-b}}\sqrt{2-b}} + \\ & \frac{\sqrt{2+b} \text{ArcTan}\left[\frac{\sqrt{2-\sqrt{2-b}}+2x}{\sqrt{2+\sqrt{2-b}}}\right]}{4\sqrt{2-\sqrt{2-b}}\sqrt{2-b}} - \frac{\sqrt{2+b} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{2-b}}+2x}{\sqrt{2-\sqrt{2-b}}}\right]}{4\sqrt{2+\sqrt{2-b}}\sqrt{2-b}} + \\ & \frac{\sqrt{2-\sqrt{2-b}} \text{Log}\left[1-\sqrt{2-\sqrt{2-b}} x+x^2\right]}{8\sqrt{2-b}} - \frac{\sqrt{2-\sqrt{2-b}} \text{Log}\left[1+\sqrt{2-\sqrt{2-b}} x+x^2\right]}{8\sqrt{2-b}} - \\ & \frac{\sqrt{2+\sqrt{2-b}} \text{Log}\left[1-\sqrt{2+\sqrt{2-b}} x+x^2\right]}{8\sqrt{2-b}} + \frac{\sqrt{2+\sqrt{2-b}} \text{Log}\left[1+\sqrt{2+\sqrt{2-b}} x+x^2\right]}{8\sqrt{2-b}} \end{aligned}$$

Result (type 7, 57 leaves):

$$-\frac{1}{4} \text{RootSum}\left[1+bx \#1^4+\#1^8 \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1] \#1^4}{b \#1^3+2 \#1^7} \&\right]$$

**Problem 21: Result is not expressed in closed-form.**

$$\int \frac{1-x^4}{1+3x^4+x^8} dx$$

Optimal (type 3, 411 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1-\frac{2^{3/4} x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}} + \frac{(3+\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1+\frac{2^{3/4} x}{(3-\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}} + \\
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1-\frac{2^{3/4} x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}} - \frac{(3-\sqrt{5})^{1/4} \operatorname{ArcTan}\left[1+\frac{2^{3/4} x}{(3+\sqrt{5})^{1/4}}\right]}{2 \times 2^{3/4}} - \\
 & \frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})-2(2(3-\sqrt{5}))^{1/4} x+2 x^2}\right]}{4 \times 2^{3/4}} + \\
 & \frac{(3+\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3-\sqrt{5})+2(2(3-\sqrt{5}))^{1/4} x+2 x^2}\right]}{4 \times 2^{3/4}} + \\
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})-2(2(3+\sqrt{5}))^{1/4} x+2 x^2}\right]}{4 \times 2^{3/4}} - \\
 & \frac{(3-\sqrt{5})^{1/4} \operatorname{Log}\left[\sqrt{2(3+\sqrt{5})+2(2(3+\sqrt{5}))^{1/4} x+2 x^2}\right]}{4 \times 2^{3/4}}
 \end{aligned}$$

Result (type 7, 57 leaves):

$$-\frac{1}{4} \operatorname{RootSum}\left[1+3 \#1^4+\#1^8 \&, \frac{-\operatorname{Log}[x-\#1]+\operatorname{Log}[x-\#1] \#1^4}{3 \#1^3+2 \#1^7} \&\right]$$

**Problem 23: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{1-x^4}{1+x^4+x^8} dx$$

Optimal (type 3, 140 leaves, 19 steps):

$$\begin{aligned}
 & -\frac{1}{4} \sqrt{3} \operatorname{ArcTan}\left[\frac{1-2 x}{\sqrt{3}}\right] + \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}-2 x] + \frac{1}{4} \sqrt{3} \operatorname{ArcTan}\left[\frac{1+2 x}{\sqrt{3}}\right] - \frac{1}{4} \operatorname{ArcTan}[\sqrt{3}+2 x] + \\
 & \frac{1}{8} \operatorname{Log}[1-x+x^2] - \frac{1}{8} \operatorname{Log}[1+x+x^2] - \frac{1}{8} \sqrt{3} \operatorname{Log}[1-\sqrt{3} x+x^2] + \frac{1}{8} \sqrt{3} \operatorname{Log}[1+\sqrt{3} x+x^2]
 \end{aligned}$$

Result (type 3, 129 leaves):

$$\begin{aligned}
 & \frac{1}{8} \left( -2 \sqrt{-2-2 i \sqrt{3}} \operatorname{ArcTan}\left[\frac{1}{2}(1-i \sqrt{3}) x\right] - 2 \sqrt{-2+2 i \sqrt{3}} \operatorname{ArcTan}\left[\frac{1}{2}(1+i \sqrt{3}) x\right] + \right. \\
 & \left. 2 \sqrt{3} \operatorname{ArcTan}\left[\frac{-1+2 x}{\sqrt{3}}\right] + 2 \sqrt{3} \operatorname{ArcTan}\left[\frac{1+2 x}{\sqrt{3}}\right] + \operatorname{Log}[1-x+x^2] - \operatorname{Log}[1+x+x^2] \right)
 \end{aligned}$$

**Problem 25: Result is not expressed in closed-form.**

$$\int \frac{1-x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 355 leaves, 19 steps):

$$\begin{aligned} & -\frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}-2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2-\sqrt{3}}+2x}{\sqrt{2+\sqrt{3}}}\right]}{4\sqrt{3(2-\sqrt{3})}} - \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2x}{\sqrt{2-\sqrt{3}}}\right]}{4\sqrt{3(2+\sqrt{3})}} + \\ & \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1-\sqrt{2-\sqrt{3}}x+x^2\right] - \frac{1}{8}\sqrt{\frac{1}{3}(2-\sqrt{3})}\text{Log}\left[1+\sqrt{2-\sqrt{3}}x+x^2\right] - \\ & \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1-\sqrt{2+\sqrt{3}}x+x^2\right] + \frac{1}{8}\sqrt{\frac{1}{3}(2+\sqrt{3})}\text{Log}\left[1+\sqrt{2+\sqrt{3}}x+x^2\right] \end{aligned}$$

Result (type 7, 57 leaves):

$$-\frac{1}{4}\text{RootSum}\left[1-\#1^4+\#1^8\ \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1]\#1^4}{-\#1^3+2\#1^7}\ \&\right]$$

**Problem 28: Result is not expressed in closed-form.**

$$\int \frac{1-x^4}{1-4x^4+x^8} dx$$

Optimal (type 3, 165 leaves, 7 steps):

$$\begin{aligned} & \frac{\text{ArcTan}\left[\frac{2^{1/4}x}{\sqrt{-1+\sqrt{3}}}\right]}{2\times 2^{1/4}\sqrt{3(-1+\sqrt{3})}} + \frac{\text{ArcTan}\left[\frac{2^{1/4}x}{\sqrt{1+\sqrt{3}}}\right]}{2\times 2^{1/4}\sqrt{3(1+\sqrt{3})}} + \frac{\text{ArcTanh}\left[\frac{2^{1/4}x}{\sqrt{-1+\sqrt{3}}}\right]}{2\times 2^{1/4}\sqrt{3(-1+\sqrt{3})}} + \frac{\text{ArcTanh}\left[\frac{2^{1/4}x}{\sqrt{1+\sqrt{3}}}\right]}{2\times 2^{1/4}\sqrt{3(1+\sqrt{3})}} \end{aligned}$$

Result (type 7, 55 leaves):

$$-\frac{1}{8}\text{RootSum}\left[1-4\#1^4+\#1^8\ \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1]\#1^4}{-2\#1^3+\#1^7}\ \&\right]$$

**Problem 29: Result is not expressed in closed-form.**

$$\int \frac{1-x^4}{1-5x^4+x^8} dx$$

Optimal (type 3, 169 leaves, 7 steps):



$$\frac{\text{ArcTan}\left[\sqrt{\frac{2}{-\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{14(-\sqrt{3}+\sqrt{7})}} + \frac{\text{ArcTan}\left[\sqrt{\frac{2}{\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{14(\sqrt{3}+\sqrt{7})}} + \frac{\text{ArcTanh}\left[\sqrt{\frac{2}{-\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{14(-\sqrt{3}+\sqrt{7})}} + \frac{\text{ArcTanh}\left[\sqrt{\frac{2}{\sqrt{3}+\sqrt{7}}} x\right]}{\sqrt{14(\sqrt{3}+\sqrt{7})}}$$

Result (type 7, 57 leaves):

$$-\frac{1}{4} \text{RootSum}\left[1-5 \#1^4+\#1^8 \&, \frac{-\text{Log}[x-\#1]+\text{Log}[x-\#1] \#1^4}{-5 \#1^3+2 \#1^7} \&\right]$$

**Problem 31: Result is not expressed in closed-form.**

$$\int \frac{-1+\sqrt{3}+2 x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 135 leaves, 9 steps):

$$-\frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2 x}{\sqrt{2-\sqrt{3}}}\right]}{\sqrt{2}} + \frac{\text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2 x}{\sqrt{2-\sqrt{3}}}\right]}{\sqrt{2}} - \frac{\text{Log}\left[1-\sqrt{2-\sqrt{3}} x+x^2\right]}{2 \sqrt{2}} + \frac{\text{Log}\left[1+\sqrt{2-\sqrt{3}} x+x^2\right]}{2 \sqrt{2}}$$

Result (type 7, 71 leaves):

$$\frac{1}{4} \text{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{-\text{Log}[x-\#1]+\sqrt{3} \text{Log}[x-\#1]+2 \text{Log}[x-\#1] \#1^4}{-\#1^3+2 \#1^7} \&\right]$$

**Problem 32: Result is not expressed in closed-form.**

$$\int \frac{1+(1+\sqrt{3}) x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 164 leaves, 9 steps):

$$-\frac{1}{2} \sqrt{2+\sqrt{3}} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2 x}{\sqrt{2-\sqrt{3}}}\right] + \frac{1}{2} \sqrt{2+\sqrt{3}} \text{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2 x}{\sqrt{2-\sqrt{3}}}\right] - \frac{1}{4} \sqrt{2+\sqrt{3}} \text{Log}\left[1-\sqrt{2-\sqrt{3}} x+x^2\right] + \frac{1}{4} \sqrt{2+\sqrt{3}} \text{Log}\left[1+\sqrt{2-\sqrt{3}} x+x^2\right]$$

Result (type 7, 72 leaves):

$$\frac{1}{4} \text{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{\text{Log}[x-\#1]+\text{Log}[x-\#1] \#1^4+\sqrt{3} \text{Log}[x-\#1] \#1^4}{-\#1^3+2 \#1^7} \&\right]$$

**Problem 33: Result is not expressed in closed-form.**

$$\int \frac{3-2 \sqrt{3}+(-3+\sqrt{3}) x^4}{1-x^4+x^8} dx$$

Optimal (type 3, 180 leaves, 9 steps):

$$\frac{1}{2} \sqrt{3(2-\sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}-2 x}{\sqrt{2-\sqrt{3}}}\right]-\frac{1}{2} \sqrt{3(2-\sqrt{3})} \operatorname{ArcTan}\left[\frac{\sqrt{2+\sqrt{3}}+2 x}{\sqrt{2-\sqrt{3}}}\right]+$$

$$\frac{1}{4} \sqrt{3(2-\sqrt{3})} \operatorname{Log}\left[1-\sqrt{2-\sqrt{3}} x+x^2\right]-\frac{1}{4} \sqrt{3(2-\sqrt{3})} \operatorname{Log}\left[1+\sqrt{2-\sqrt{3}} x+x^2\right]$$

Result (type 7, 89 leaves):

$$\frac{1}{4} \operatorname{RootSum}\left[1-\#1^4+\#1^8 \&, \frac{1}{-\#1^3+2 \#1^7}\left(3 \operatorname{Log}[x-\#1]-2 \sqrt{3} \operatorname{Log}[x-\#1]-3 \operatorname{Log}[x-\#1] \#1^4+\sqrt{3} \operatorname{Log}[x-\#1] \#1^4\right) \&\right]$$

**Problem 39: Result is not expressed in closed-form.**

$$\int \frac{d+\frac{e}{x^3}}{c+\frac{a}{x^6}+\frac{b}{x^3}} dx$$

Optimal (type 3, 716 leaves, 15 steps):

$$\frac{d x}{c} + \frac{\left(b d - c e - \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{\left(b - \sqrt{b^2 - 4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{2/3}} +$$

$$\frac{\left(b d - c e + \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right) \operatorname{ArcTan}\left[\frac{1 - \frac{2 \cdot 2^{1/3} c^{1/3} x}{\left(b + \sqrt{b^2 - 4 a c}\right)^{1/3}}}{\sqrt{3}}\right]}{2^{1/3} \sqrt{3} c^{4/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{2/3}} -$$

$$\frac{\left(b d - c e - \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b - \sqrt{b^2 - 4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{2/3}} -$$

$$\frac{\left(b d - c e + \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right) \operatorname{Log}\left[\left(b + \sqrt{b^2 - 4 a c}\right)^{1/3} + 2^{1/3} c^{1/3} x\right]}{3 \times 2^{1/3} c^{4/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{2/3}} + \left(\left(b d - c e - \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right)\right.$$

$$\left. \operatorname{Log}\left[\left(b - \sqrt{b^2 - 4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} \left(b - \sqrt{b^2 - 4 a c}\right)^{2/3}\right) + \left(\left(b d - c e + \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}}\right)\right.$$

$$\left. \operatorname{Log}\left[\left(b + \sqrt{b^2 - 4 a c}\right)^{2/3} - 2^{1/3} c^{1/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{1/3} x + 2^{2/3} c^{2/3} x^2\right]\right) /$$

$$\left(6 \times 2^{1/3} c^{4/3} \left(b + \sqrt{b^2 - 4 a c}\right)^{2/3}\right)$$

Result (type 7, 88 leaves):

$$\frac{d x}{c} - \frac{\operatorname{RootSum}\left[a + b \#1^3 + c \#1^6 \&, \frac{a d \operatorname{Log}[x - \#1] + b d \operatorname{Log}[x - \#1] \#1^3 - c e \operatorname{Log}[x - \#1] \#1^3}{b \#1^2 + 2 c \#1^5} \&\right]}{3 c}$$

**Problem 41: Result is not expressed in closed-form.**

$$\int \frac{d + \frac{e}{x^4}}{c + \frac{a}{x^8} + \frac{b}{x^4}} dx$$

Optimal (type 3, 433 leaves, 9 steps):

$$\frac{d x}{c} + \frac{\left( b d - c e + \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}} \right) \text{ArcTan} \left[ \frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}} \right]}{2 \times 2^{1/4} c^{5/4} (-b - \sqrt{b^2 - 4 a c})^{3/4}} +$$

$$\frac{\left( b d - c e - \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}} \right) \text{ArcTan} \left[ \frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}} \right]}{2 \times 2^{1/4} c^{5/4} (-b + \sqrt{b^2 - 4 a c})^{3/4}} +$$

$$\frac{\left( b d - c e + \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}} \right) \text{ArcTanh} \left[ \frac{2^{1/4} c^{1/4} x}{(-b - \sqrt{b^2 - 4 a c})^{1/4}} \right]}{2 \times 2^{1/4} c^{5/4} (-b - \sqrt{b^2 - 4 a c})^{3/4}} +$$

$$\frac{\left( b d - c e - \frac{b^2 d - 2 a c d - b c e}{\sqrt{b^2 - 4 a c}} \right) \text{ArcTanh} \left[ \frac{2^{1/4} c^{1/4} x}{(-b + \sqrt{b^2 - 4 a c})^{1/4}} \right]}{2 \times 2^{1/4} c^{5/4} (-b + \sqrt{b^2 - 4 a c})^{3/4}}$$

Result (type 7, 88 leaves):

$$\frac{d x}{c} - \frac{\text{RootSum} \left[ a + b \#1^4 + c \#1^8 \&, \frac{a d \text{Log}[x-\#1] + b d \text{Log}[x-\#1] \#1^4 - c e \text{Log}[x-\#1] \#1^4}{b \#1^3 + 2 c \#1^7} \& \right]}{4 c}$$

### Problem 58: Unable to integrate problem.

$$\int \frac{1}{(d + e x^n) \sqrt{a + c x^{2n}}} dx$$

Optimal (type 6, 171 leaves, 6 steps):

$$\frac{x \sqrt{1 + \frac{c x^{2n}}{a}} \text{AppellF1} \left[ \frac{1}{2n}, \frac{1}{2}, 1, \frac{1}{2} \left( 2 + \frac{1}{n} \right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2} \right]}{d \sqrt{a + c x^{2n}}} -$$

$$\frac{e x^{1+n} \sqrt{1 + \frac{c x^{2n}}{a}} \text{AppellF1} \left[ \frac{1+n}{2n}, \frac{1}{2}, 1, \frac{1}{2} \left( 3 + \frac{1}{n} \right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2} \right]}{d^2 (1+n) \sqrt{a + c x^{2n}}}$$

Result (type 8, 25 leaves):

$$\int \frac{1}{(d + e x^n) \sqrt{a + c x^{2n}}} dx$$

### Problem 63: Unable to integrate problem.

$$\int \frac{(a + c x^{2n})^p}{d + e x^n} dx$$

Optimal (type 6, 167 leaves, 6 steps):

$$\frac{1}{d} x (a + c x^{2n})^p \left(1 + \frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1}{2n}, -p, 1, \frac{1}{2} \left(2 + \frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] - \frac{1}{d^2 (1+n)}$$

$$e x^{1+n} (a + c x^{2n})^p \left(1 + \frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1+n}{2n}, -p, 1, \frac{1}{2} \left(3 + \frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right]$$

Result (type 8, 23 leaves):

$$\int \frac{(a + c x^{2n})^p}{d + e x^n} dx$$

### Problem 64: Unable to integrate problem.

$$\int \frac{(a + c x^{2n})^p}{(d + e x^n)^2} dx$$

Optimal (type 6, 261 leaves, 8 steps):

$$\frac{1}{d^4 (1 + 2n)}$$

$$e^2 x^{1+2n} (a + c x^{2n})^p \left(1 + \frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1}{2} \left(2 + \frac{1}{n}\right), -p, 2, \frac{1}{2} \left(4 + \frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] +$$

$$\frac{1}{d^2} x (a + c x^{2n})^p \left(1 + \frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1}{2n}, -p, 2, \frac{1}{2} \left(2 + \frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] - \frac{1}{d^3 (1+n)}$$

$$2 e x^{1+n} (a + c x^{2n})^p \left(1 + \frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1+n}{2n}, -p, 2, \frac{1}{2} \left(3 + \frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right]$$

Result (type 8, 23 leaves):

$$\int \frac{(a + c x^{2n})^p}{(d + e x^n)^2} dx$$

### Problem 65: Unable to integrate problem.

$$\int \frac{(a + c x^{2n})^p}{(d + e x^n)^3} dx$$

Optimal (type 6, 357 leaves, 10 steps):

$$\frac{1}{d^5 (1+2n)} 3 e^2 x^{1+2n} (a+c x^{2n})^p \left(1+\frac{c x^{2n}}{a}\right)^{-p}$$

$$\text{AppellF1}\left[\frac{1}{2}\left(2+\frac{1}{n}\right), -p, 3, \frac{1}{2}\left(4+\frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] - \frac{1}{d^6 (1+3n)}$$

$$e^3 x^{1+3n} (a+c x^{2n})^p \left(1+\frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1}{2}\left(3+\frac{1}{n}\right), -p, 3, \frac{1}{2}\left(5+\frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] +$$

$$\frac{1}{d^3} x (a+c x^{2n})^p \left(1+\frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1}{2n}, -p, 3, \frac{1}{2}\left(2+\frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right] - \frac{1}{d^4 (1+n)}$$

$$3 e x^{1+n} (a+c x^{2n})^p \left(1+\frac{c x^{2n}}{a}\right)^{-p} \text{AppellF1}\left[\frac{1+n}{2n}, -p, 3, \frac{1}{2}\left(3+\frac{1}{n}\right), -\frac{c x^{2n}}{a}, \frac{e^2 x^{2n}}{d^2}\right]$$

Result (type 8, 23 leaves):

$$\int \frac{(a+c x^{2n})^p}{(d+e x^n)^3} dx$$

### Problem 73: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(d+e x^n)^2 (a+b x^n+c x^{2n})} dx$$

Optimal (type 5, 368 leaves, 7 steps):

$$-\left(\left(c\left(2c^2d^2+b\left(b+\sqrt{b^2-4ac}\right)\right)e^2-2ce\left(bd+\sqrt{b^2-4ac}d+ae\right)\right) \times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1+\frac{1}{n}, -\frac{2cx^n}{b-\sqrt{b^2-4ac}}\right]\right) / \left(\left(b^2-4ac-b\sqrt{b^2-4ac}\right)\left(cd^2-bde+ae^2\right)^2\right) -$$

$$\left(c\left(2c^2d^2+b\left(b-\sqrt{b^2-4ac}\right)\right)e^2-2ce\left(bd-\sqrt{b^2-4ac}d+ae\right)\right) \times$$

$$\text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1+\frac{1}{n}, -\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] /$$

$$\left(\left(b^2-4ac+b\sqrt{b^2-4ac}\right)\left(cd^2-bde+ae^2\right)^2\right) +$$

$$\frac{e^2(2cd-be) \times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1+\frac{1}{n}, -\frac{ex^n}{d}\right]}{d\left(cd^2-bde+ae^2\right)^2} +$$

$$\frac{e^2 \times \text{Hypergeometric2F1}\left[2, \frac{1}{n}, 1+\frac{1}{n}, -\frac{ex^n}{d}\right]}{d^2\left(cd^2-bde+ae^2\right)}$$

Result (type 5, 2302 leaves):

$$\frac{(ae^2-cd^2n+bden-ae^2n) \times}{ad^2(cd^2-bde+ae^2)n} +$$

$$\frac{(-ae^2+cd^2n-bden+ae^2n) \times}{ad^2(cd^2-bde+ae^2)n} + \frac{e^2x}{d(cd^2-bde+ae^2)n(d+ex^n)} +$$

$$\begin{aligned}
 & \left( e^2 (-c d^2 + b d e - a e^2 + 3 c d^2 n - 2 b d e n + a e^2 n) \times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d}\right] \right) / \\
 & \left( d^2 (c d^2 - b d e + a e^2)^2 n \right) - \left( 2 c^2 d e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)}\right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)}\right] \right) \right) / \\
 & \left( c d^2 - b d e + a e^2 \right)^2 + \left( b c e^2 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)}\right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)}\right] \right) \right) / \\
 & \left( c d^2 - b d e + a e^2 \right)^2 - \left( c^2 d^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)}\right] \right) \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) + \\
 & \quad \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right.$$

$$(cd^2 - bde + ae^2)^2 + \left( 2bcde x \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right.$$

$$\left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \right] \right) \left/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right.$$

$$\left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \left/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right.$$

$$(cd^2 - bde + ae^2)^2 - \left( b^2 e^2 x \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right.$$

$$\left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \right] \right) \left/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right.$$

$$\left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \left/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right.$$



$$\begin{aligned}
 & (c d^2 - b d e + a e^2)^2 + \left( a c e^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) / \right. \\
 & \quad \left. \left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) / \right. \\
 & \quad \left. \left. \left( \frac{b \left( -b + \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b + \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) \right) \right) / (c d^2 - b d e + a e^2)^2
 \end{aligned}$$

**Problem 74: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d + e x^n)^3 (a + b x^n + c x^{2n})} dx$$

Optimal (type 5, 552 leaves, 8 steps):

$$\begin{aligned}
 & - \left( \left( c \left( 2 c^3 d^3 - b^2 \left( b + \sqrt{b^2 - 4 a c} \right) e^3 - 3 c^2 d e \left( b d + \sqrt{b^2 - 4 a c} d + 2 a e \right) + \right. \right. \right. \\
 & \quad \left. \left. \left. c e^2 \left( 3 b^2 d + a \sqrt{b^2 - 4 a c} e + 3 b \left( \sqrt{b^2 - 4 a c} d + a e \right) \right) \right) \right) \right) \\
 & \quad \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] / \\
 & \quad \left( \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) \left( c d^2 - b d e + a e^2 \right)^3 \right) - \\
 & \left( c \left( 2 c^3 d^3 - b^2 \left( b - \sqrt{b^2 - 4 a c} \right) e^3 - 3 c^2 d e \left( b d - \sqrt{b^2 - 4 a c} d + 2 a e \right) + \right. \right. \\
 & \quad \left. \left. c e^2 \left( 3 b^2 d - 3 b \sqrt{b^2 - 4 a c} d + 3 a b e - a \sqrt{b^2 - 4 a c} e \right) \right) \right) \\
 & \quad \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] / \\
 & \quad \left( \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) \left( c d^2 - b d e + a e^2 \right)^3 \right) + \\
 & \left( e^2 \left( 3 c^2 d^2 + b^2 e^2 - c e \left( 3 b d + a e \right) \right) \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right] \right) / \\
 & \quad \left( d \left( c d^2 - b d e + a e^2 \right)^3 \right) + \\
 & \frac{e^2 \left( 2 c d - b e \right) \times \text{Hypergeometric2F1} \left[ 2, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d^2 \left( c d^2 - b d e + a e^2 \right)^2} + \\
 & \frac{e^2 \times \text{Hypergeometric2F1} \left[ 3, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d^3 \left( c d^2 - b d e + a e^2 \right)}
 \end{aligned}$$

Result (type 5, 4111 leaves):

$$\begin{aligned}
 & \left( \left( -a c d^2 e^2 + a b d e^3 - a^2 e^4 + 7 a c d^2 e^2 n - 5 a b d e^3 n + 3 a^2 e^4 n - 2 c^2 d^4 n^2 + 4 b c d^3 e n^2 - 2 b^2 d^2 e^2 n^2 - \right. \right. \\
 & \quad \left. \left. 4 a c d^2 e^2 n^2 + 4 a b d e^3 n^2 - 2 a^2 e^4 n^2 \right) x \right) / \left( 2 a d^3 \left( c d^2 - b d e + a e^2 \right)^2 n^2 \right) + \\
 & \left( \left( a c d^2 e^2 - a b d e^3 + a^2 e^4 - 7 a c d^2 e^2 n + 5 a b d e^3 n - 3 a^2 e^4 n + 2 c^2 d^4 n^2 - \right. \right. \\
 & \quad \left. \left. 4 b c d^3 e n^2 + 2 b^2 d^2 e^2 n^2 + 4 a c d^2 e^2 n^2 - 4 a b d e^3 n^2 + 2 a^2 e^4 n^2 \right) x \right) / \\
 & \quad \left( 2 a d^3 \left( c d^2 - b d e + a e^2 \right)^2 n^2 \right) + \frac{e^2 x}{2 d \left( c d^2 - b d e + a e^2 \right) n \left( d + e x^n \right)^2} + \\
 & \frac{\left( -c d^2 e^2 + b d e^3 - a e^4 + 6 c d^2 e^2 n - 4 b d e^3 n + 2 a e^4 n \right) x}{2 d^2 \left( c d^2 - b d e + a e^2 \right)^2 n^2 \left( d + e x^n \right)} + \\
 & \left( \left( c^2 d^4 e^2 - 2 b c d^3 e^3 + b^2 d^2 e^4 + 2 a c d^2 e^4 - 2 a b d e^5 + a^2 e^6 - 7 c^2 d^4 e^2 n + 12 b c d^3 e^3 n - 5 b^2 d^2 e^4 n - \right. \right. \\
 & \quad \left. \left. 10 a c d^2 e^4 n + 8 a b d e^5 n - 3 a^2 e^6 n + 12 c^2 d^4 e^2 n^2 - 16 b c d^3 e^3 n^2 + 6 b^2 d^2 e^4 n^2 + \right. \right. \\
 & \quad \left. \left. 6 a c d^2 e^4 n^2 - 6 a b d e^5 n^2 + 2 a^2 e^6 n^2 \right) \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 d^3 (c d^2 - b d e + a e^2)^3 n^2 \right) - \left( 3 c^3 d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( c d^2 - b d e + a e^2 \right)^3 + \left( 3 b c^2 d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( c d^2 - b d e + a e^2 \right)^3 - \left( b^2 c e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( c d^2 - b d e + a e^2 \right)^3 + \left( a c^2 e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \\
 & (cd^2 - bde + ae^2)^3 - \left(c^3 d^3 x \left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right) + \right. \\
 & \left. \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right) \right) \Bigg) \Bigg/ \\
 & (cd^2 - bde + ae^2)^3 + \left(3bc^2 d^2 e x \left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right) + \right. \\
 & \left. \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right) \right) \Bigg) \Bigg) \Bigg/
 \end{aligned}$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/$$

$$(cd^2 - bde + ae^2)^3 - \left( 3b^2cde^2 x \left( \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right.$$

$$\left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/$$

$$(cd^2 - bde + ae^2)^3 + \left( 3ac^2de^2 x \left( \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right.$$

$$\left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/$$

$$\begin{aligned}
 & (c d^2 - b d e + a e^2)^3 + \left( b^3 e^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right)^2 \right) + \\
 & \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. \frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right)^2 \right) \Bigg) / \\
 & (c d^2 - b d e + a e^2)^3 - \left( 2 a b c e^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \left. \left. \left. \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) \right) \Bigg) / (c d^2 - b d e + a e^2)^3
 \end{aligned}$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int \frac{(d+e x^n)^3}{(a+b x^n+c x^{2 n})^2} dx$$

Optimal (type 5, 750 leaves, 9 steps):

$$\begin{aligned} & \left( x (b^2 c d^3 - 2 a c d (c d^2 - 3 a e^2) - a b e (3 c d^2 + a e^2) - (a b^2 e^3 + 2 a c e (3 c d^2 - a e^2) - b c d (c d^2 + 3 a e^2)) x^n) / \right. \\ & \left. (a c (b^2 - 4 a c) n (a + b x^n + c x^{2 n})) + \right. \\ & \left. \frac{e^2 \left( e + \frac{6 c d - 3 b e}{\sqrt{b^2 - 4 a c}} \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right]}{c (b - \sqrt{b^2 - 4 a c})} + \right. \\ & \left( \left( (a b^2 e^3 + 2 a c e (3 c d^2 - a e^2) - b c d (c d^2 + 3 a e^2)) (1 - n) + \right. \right. \\ & \left. \frac{1}{\sqrt{b^2 - 4 a c}} (b^2 c d (3 a e^2 (1 - 3 n) - c d^2 (1 - n)) - a b^3 e^3 (1 - 3 n) + \right. \\ & \left. \left. 4 a c^2 d (c d^2 - 3 a e^2) (1 - 2 n) + 2 a b c e (a e^2 (2 - 5 n) + 3 c d^2 n) \right) \right) x \\ & \left. \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / (a c (b^2 - 4 a c) (b - \sqrt{b^2 - 4 a c}) n) + \\ & \frac{e^2 \left( e - \frac{3 (2 c d - b e)}{\sqrt{b^2 - 4 a c}} \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right]}{c (b + \sqrt{b^2 - 4 a c})} + \\ & \left( \left( (a b^2 e^3 + 2 a c e (3 c d^2 - a e^2) - b c d (c d^2 + 3 a e^2)) (1 - n) - \right. \right. \\ & \left. \frac{1}{\sqrt{b^2 - 4 a c}} (b^2 c d (3 a e^2 (1 - 3 n) - c d^2 (1 - n)) - a b^3 e^3 (1 - 3 n) + \right. \\ & \left. \left. 4 a c^2 d (c d^2 - 3 a e^2) (1 - 2 n) + 2 a b c e (a e^2 (2 - 5 n) + 3 c d^2 n) \right) \right) x \\ & \left. \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / (a c (b^2 - 4 a c) (b + \sqrt{b^2 - 4 a c}) n) \end{aligned}$$

Result (type 5, 5537 leaves):

$$\begin{aligned} & \left( (-b^2 c d^3 + 2 a c^2 d^3 + 3 a b c d^2 e - 6 a^2 c d e^2 + a^2 b e^3 + b^2 c d^3 n - 4 a c^2 d^3 n) x \right) / \\ & (a^2 c (-b^2 + 4 a c) n) + \\ & \left( (b^2 c d^3 - 2 a c^2 d^3 - 3 a b c d^2 e + 6 a^2 c d e^2 - a^2 b e^3 - b^2 c d^3 n + 4 a c^2 d^3 n) x \right) / \\ & (a^2 c (-b^2 + 4 a c) n) - \\ & \left( x (b^2 c d^3 - 2 a c^2 d^3 - 3 a b c d^2 e + 6 a^2 c d e^2 - a^2 b e^3 + b c^2 d^3 x^n - 6 a c^2 d^2 e x^n + \right. \\ & \left. 3 a b c d e^2 x^n - a b^2 e^3 x^n + 2 a^2 c e^3 x^n) \right) / (a c (-b^2 + 4 a c) n (a + b x^n + c x^{2 n})) - \\ & \frac{1}{a (-b^2 + 4 a c)} b c d^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right) \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \\
 & \frac{1}{-b^2+4ac} 6cd^2e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \left. \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] - \right. \\
 & \left. \frac{1}{-b^2+4ac} 3bde^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \left. \left. \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \right. \right. \\
 & \left. \left. \frac{1}{-b^2+4ac} 2ae^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.
 \end{aligned}$$



$$\left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] +$$

$$\frac{1}{a(-b^2+4ac)n} b c d^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) -$$

$$\frac{1}{(-b^2+4ac)n} 6 c d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\frac{1}{(-b^2+4ac)n} 3 b d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\frac{1}{(-b^2 + 4 a c) n} 2 a e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}}$$

$$\left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] - \right.$$

$$\frac{1}{c (-b^2 + 4 a c) n} b^2 e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n}$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{a (-b^2 + 4 a c)} b^2 d^3 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b (-b - \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b - \sqrt{b^2 - 4 a c})^2}{2 c} \right) + \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b (-b + \sqrt{b^2 - 4 a c})}{2 c} + \frac{(-b + \sqrt{b^2 - 4 a c})^2}{2 c} \right) - \frac{1}{-b^2 + 4 a c} 4 c d^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) - \frac{1}{a(-b^2+4ac)n} b^2 d^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{(-b^2+4ac)n} 2c d^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) + \frac{1}{(-b^2+4ac)n} 3 b d^2 e x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) - \frac{1}{(-b^2+4ac)n} 6 a d e^2 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) + \frac{1}{c \left( -b^2+4ac \right) n} a b e^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right)$$

**Problem 76: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d + e x^n)^2}{(a + b x^n + c x^{2n})^2} dx$$

Optimal (type 5, 543 leaves, 9 steps):

$$\frac{x (b^2 d^2 - 2 a b d e - 2 a (c d^2 - a e^2) + (b c d^2 - 4 a c d e + a b e^2) x^n)}{a (b^2 - 4 a c) n (a + b x^n + c x^{2n})} -$$

$$\frac{2 e^2 x \operatorname{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right]}{b^2 - 4 a c - b \sqrt{b^2 - 4 a c}} -$$

$$\left( \left( (b c d^2 - 4 a c d e + a b e^2) (1 - n) - \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right.$$

$$\left. \left. (b^2 (a e^2 (1 - 3 n) - c d^2 (1 - n)) + 4 a c (c d^2 - a e^2) (1 - 2 n) + 4 a b c d e n) \right) x \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right] \right) / \left( a (b^2 - 4 a c) (b - \sqrt{b^2 - 4 a c}) n \right) -$$

$$\frac{2 e^2 x \operatorname{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right]}{b^2 - 4 a c + b \sqrt{b^2 - 4 a c}} -$$

$$\left( \left( (b c d^2 - 4 a c d e + a b e^2) (1 - n) + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right.$$

$$\left. \left. (b^2 (a e^2 (1 - 3 n) - c d^2 (1 - n)) + 4 a c (c d^2 - a e^2) (1 - 2 n) + 4 a b c d e n) \right) x \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \right) / \left( a (b^2 - 4 a c) (b + \sqrt{b^2 - 4 a c}) n \right)$$

Result (type 5, 4177 leaves):

$$\frac{(-b^2 d^2 + 2 a c d^2 + 2 a b d e - 2 a^2 e^2 + b^2 d^2 n - 4 a c d^2 n) x}{a^2 (-b^2 + 4 a c) n} +$$

$$\frac{(b^2 d^2 - 2 a c d^2 - 2 a b d e + 2 a^2 e^2 - b^2 d^2 n + 4 a c d^2 n) x}{a^2 (-b^2 + 4 a c) n} -$$

$$\frac{x (b^2 d^2 - 2 a c d^2 - 2 a b d e + 2 a^2 e^2 + b c d^2 x^n - 4 a c d e x^n + a b e^2 x^n)}{a (-b^2 + 4 a c) n (a + b x^n + c x^{2n})} -$$

$$\frac{1}{a (-b^2 + 4 a c)} b c d^2 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left(-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n\right)}\right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left(-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n\right)}\right] \right) +$$

$$\begin{aligned}
 & \frac{1}{-b^2+4ac} 4c d e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] - \right. \\
 & \quad \left. \frac{1}{-b^2+4ac} b e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) + \right. \\
 & \quad \left. \frac{1}{a(-b^2+4ac)n} b c d^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] - \right. \\
 & \quad \left. \left. \frac{1}{(-b^2+4ac)n} 4c d e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \\
 & \frac{1}{(-b^2+4ac)n} b e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[ \right. \right. \\
 & \left. \left. -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{a(-b^2+4ac)} b^2 d^2 x \right. \\
 & \left. \left. \left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) / \right. \right. \\
 & \left. \left. \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c}\right) + \right. \right. \\
 & \left. \left. \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) / \right. \right. \\
 & \left. \left. \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right) \right) - \frac{1}{-b^2+4ac} 4c d^2 x \right. \\
 & \left. \left. \left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) / \right. \right.
 \end{aligned}$$



$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \Big/$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) - \frac{1}{a(-b^2+4ac)n} b^2 d^2 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Big/$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \Big/$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{(-b^2+4ac)n} 2c d^2 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Big/$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \Big/$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) + \frac{1}{(-b^2 + 4ac)n} 2bdex$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) - \frac{1}{(-b^2 + 4ac)n} 2ae^2x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right)$$

Problem 77: Result more than twice size of optimal antiderivative.

$$\int \frac{d + ex^n}{(a + bx^n + cx^{2n})^2} dx$$

Optimal (type 5, 362 leaves, 4 steps):

$$\frac{x (b^2 d - 2 a c d - a b e + c (b d - 2 a e) x^n)}{a (b^2 - 4 a c) n (a + b x^n + c x^{2n})} -$$

$$\left( c \left( 2 a \left( 2 c d (1 - 2 n) + \sqrt{b^2 - 4 a c} e (1 - n) \right) - b^2 (d - d n) - b \left( \sqrt{b^2 - 4 a c} d (1 - n) - 2 a e n \right) \right) \right.$$

$$\left. \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) /$$

$$\left( a (b^2 - 4 a c) \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) n \right) -$$

$$\left( c \left( 2 a \left( c d (2 - 4 n) - \sqrt{b^2 - 4 a c} e (1 - n) \right) - b^2 d (1 - n) + b \left( \sqrt{b^2 - 4 a c} d (1 - n) + 2 a e n \right) \right) \right.$$

$$\left. \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) /$$

$$\left( a (b^2 - 4 a c) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) n \right)$$

Result (type 5, 3152 leaves):

$$\frac{(-b^2 d + 2 a c d + a b e + b^2 d n - 4 a c d n) x}{a^2 (-b^2 + 4 a c) n} +$$

$$\frac{(b^2 d - 2 a c d - a b e - b^2 d n + 4 a c d n) x}{a^2 (-b^2 + 4 a c) n} + \frac{x (-b^2 d + 2 a c d + a b e - b c d x^n + 2 a c e x^n)}{a (-b^2 + 4 a c) n (a + b x^n + c x^{2n})} -$$

$$\frac{1}{a (-b^2 + 4 a c)} b c d x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) +$$

$$\frac{1}{-b^2 + 4 a c} 2 c e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right.$$

$$\left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] +$$

$$\frac{1}{a(-b^2+4ac)n} b c d x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) -$$

$$\frac{1}{(-b^2+4ac)n} 2 c e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ \right. \right.$$

$$\left. -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n}$$

$$\text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{a(-b^2+4ac)} b^2 d x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) - \frac{1}{-b^2 + 4ac} 4cdx$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) - \frac{1}{a(-b^2 + 4ac)n} b^2 dx$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) + \frac{1}{(-b^2 + 4ac)n} 2cdx$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{(-b^2+4ac)n} b e x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right)$$

**Problem 78: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d+e x^n) (a+b x^n+c x^{2n})^2} dx$$

Optimal (type 5, 726 leaves, 10 steps):

$$\begin{aligned}
 & \frac{x (b^2 c d - 2 a c^2 d - b^3 e + 3 a b c e + c (b c d - b^2 e + 2 a c e) x^n)}{a (b^2 - 4 a c) (c d^2 - b d e + a e^2) n (a + b x^n + c x^{2 n})} - \\
 & \left( c e^2 \left( 2 c d - \left( b + \sqrt{b^2 - 4 a c} \right) e \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^2 \right) - \\
 & \left( c \left( \frac{2 a b c e (2 - 3 n) - 4 a c^2 d (1 - 2 n) + b^2 c d (1 - n) - b^3 e (1 - n)}{\sqrt{b^2 - 4 a c}} + (b c d - b^2 e + 2 a c e) (1 - n) \right) \right. \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( a (b^2 - 4 a c) \left( b - \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2) n \right) - \\
 & \left( c e^2 \left( 2 c d - \left( b - \sqrt{b^2 - 4 a c} \right) e \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^2 \right) + \\
 & \left( c \left( b c \left( 2 a e (2 - 3 n) - \sqrt{b^2 - 4 a c} d (1 - n) \right) - 2 a c \left( 2 c d (1 - 2 n) + \sqrt{b^2 - 4 a c} e (1 - n) \right) - \right. \right. \\
 & \quad \left. \left. b^3 e (1 - n) + b^2 \left( c d + \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) \right. \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( a (b^2 - 4 a c) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2) n \right) + \\
 & \frac{e^4 x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d (c d^2 - b d e + a e^2)^2}
 \end{aligned}$$

Result (type 5, 11767 leaves):

$$\begin{aligned}
 & \left( (-b^2 c d^2 + 2 a c^2 d^2 + b^3 d e - 3 a b c d e + b^2 c d^2 n - 4 a c^2 d^2 n - b^3 d e n + \right. \\
 & \quad \left. 4 a b c d e n + a b^2 e^2 n - 4 a^2 c e^2 n) x \right) / \left( a^2 (-b^2 + 4 a c) d (c d^2 - b d e + a e^2) n \right) + \\
 & \left( (b^2 c d^2 - 2 a c^2 d^2 - b^3 d e + 3 a b c d e - b^2 c d^2 n + 4 a c^2 d^2 n + b^3 d e n - 4 a b c d e n - \right. \\
 & \quad \left. a b^2 e^2 n + 4 a^2 c e^2 n) x \right) / \left( a^2 (-b^2 + 4 a c) d (c d^2 - b d e + a e^2) n \right) - \\
 & \frac{x (b^2 c d - 2 a c^2 d - b^3 e + 3 a b c e + b c^2 d x^n - b^2 c e x^n + 2 a c^2 e x^n)}{a (-b^2 + 4 a c) (c d^2 - b d e + a e^2) n (a + b x^n + c x^{2 n})} + \\
 & \frac{e^4 x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d (c d^2 - b d e + a e^2)^2} -
 \end{aligned}$$

$$\left( b c^3 d^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right) \right)^{-1/n} \right)$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \Bigg) \Bigg/ \\
 & (a(-b^2+4ac)(cd^2-bde+ae^2)^2) + \\
 & \left(2b^2c^2d^2ex^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4ac}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right.\right. \\
 & \left.\left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right) \Bigg/ \\
 & (a(-b^2+4ac)(cd^2-bde+ae^2)^2) - \\
 & \left(2c^3d^2ex^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4ac}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right.\right. \\
 & \left.\left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right) \Bigg/ \\
 & ((-b^2+4ac)(cd^2-bde+ae^2)^2) - \left(b^3cde^2x^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4ac}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.
 \end{aligned}$$



$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left. \left. \left. \left. \left. \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) \right) \right) \right) \Big/ \\
 & (a(-b^2+4ac)(cd^2-bde+ae^2)^2) + \\
 & \left( bc^2de^2x^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \left. \left. \left. \left. \left. \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) \right) \right) \right) \Big/ \\
 & ((-b^2+4ac)(cd^2-bde+ae^2)^2) + \left( 2b^2ce^3x^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \left. \left. \left. \left. \left. \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) \right) \right) \right) \Big/ \\
 & ((-b^2+4ac)(cd^2-bde+ae^2)^2) - \left( 6a^2ce^3x^{1+n}(x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.
 \end{aligned}$$

$$\left( \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg| \Bigg|$$

$$\left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 \right) + \left( bc^3 d^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg| \Bigg|$$

$$\left( a (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 n \right) -$$

$$\left( 2b^2 c^2 d^2 e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg| \Bigg|$$

$$\left( a (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 n \right) +$$

$$\left( 2c^3 d^2 e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \Bigg/$$

$$\left( (-b^2+4ac) (cd^2-bde+ae^2)^2 n \right) +$$

$$\left( b^3 c d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( a(-b^2+4ac) (cd^2-bde+ae^2)^2 n \right) -$$

$$\left( b c^2 d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( (-b^2+4ac) (cd^2-bde+ae^2)^2 n \right) - \left( b^2 c e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left( \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/$$

$$\left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 n \right) +$$

$$\left( 2ac^2 e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right.$$

$$\left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 n \right) +$$

$$\left( b^2 c^2 d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \Bigg/$$

$$\left( a (-b^2 + 4ac) (cd^2 - bde + ae^2)^2 \right) - \left( 4c^3 d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right.$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)- \\
 & \left(2b^3cd^2ex\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\right. \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)+\left(8b^3cd^2ex\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)+ \\
 & \left(b^4 d e^2 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right.\right. \\
 & \left.\left.\left.-\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)^2\right)+ \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right. \\
 & \left.\left.-\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)^2\right)\right)\right/ \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)-\left(2 b^2 c d e^2 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c}\right) + \left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right)\right) \Big/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right) - \\
 & \left(8ac^2de^2x\left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \Big/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c}\right) + \right. \\
 & \left. \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \Big/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right)\right) \Big/ \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right) - \left(2b^3e^3x\left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)+ \\
 & \left(8abc e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \\
 & \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2\right)-\left(b^2c^2d^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(a\left(-b^2+4ac\right)\left(c d^2-b d e+a e^2\right)^2 n\right)+ \\
 & \left(2 c^3 d^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right.\right. \\
 & \left.\left.\left.-\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right. \\
 & \left.\left.\left.-\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \\
 & \left.\left(\left(-b^2+4ac\right)\left(c d^2-b d e+a e^2\right)^2 n\right)+\left(2 b^3 c d^2 e x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\left/\left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2n\right)-\right. \\
 & \left(5bc^2d^2ex\left(\left(1-\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \\
 & \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right)\left/\left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2n\right)-\right. \\
 & \left(b^4d^2ex\left(\left(1-\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right/ \\
 & \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right) \right/ \\
 & \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \left. \right) \left. \right) / \left( (a(-b^2+4ac)(cd^2-bde+ae^2)^2n) + \right. \\
 & \left( 2b^2cde^2x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) \left. \right) / \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \\
 & \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) \left. \right) / \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \left. \right) \left. \right) / \\
 & \left( (-b^2+4ac)(cd^2-bde+ae^2)^2n \right) + \left( 2ac^2de^2x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2n\right)+ \\
 & \left(b^3 e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right)\right/ \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2n\right)-\left(3abc e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right\} / \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right\} / \\
 & \left.\left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right\} / \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^2n\right)
 \end{aligned}$$

**Problem 79: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(d+ex^n)^2 (a+bx^n+cx^{2n})^2} dx$$

Optimal (type 5, 1129 leaves, 11 steps):

$$\begin{aligned}
 & - \left( (x (2 b^3 c d e - 6 a b c^2 d e - b^4 e^2 - b^2 c (c d^2 - 4 a e^2) + \right. \\
 & \quad \left. 2 a c^2 (c d^2 - a e^2) + c (2 b^2 c d e - 4 a c^2 d e - b^3 e^2 - b c (c d^2 - 3 a e^2)) x^n) \right) / \\
 & \quad \left( a (b^2 - 4 a c) (c d^2 - b d e + a e^2)^2 n (a + b x^n + c x^{2 n}) \right) - \\
 & \quad \left( 2 c e^2 \left( 3 c^2 d^2 + b \left( b + \sqrt{b^2 - 4 a c} \right) e^2 - c e \left( 3 b d + 2 \sqrt{b^2 - 4 a c} d + a e \right) \right) \right. \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \quad \left( \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^3 \right) + \\
 & \quad \frac{1}{a (b^2 - 4 a c) \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^2 n} \\
 & \quad c \left( 4 a c^2 \left( e \left( a e (1 - 2 n) + \sqrt{b^2 - 4 a c} d (1 - n) \right) - c d^2 (1 - 2 n) \right) - \right. \\
 & \quad \quad b^2 c \left( e \left( a e (5 - 7 n) + 2 \sqrt{b^2 - 4 a c} d (1 - n) \right) - c d^2 (1 - n) \right) + \\
 & \quad \quad b c \left( c d \left( 4 a e (2 - 3 n) + \sqrt{b^2 - 4 a c} d (1 - n) \right) - 3 a \sqrt{b^2 - 4 a c} e^2 (1 - n) \right) + b^4 e^2 (1 - n) - \\
 & \quad \quad \left. b^3 e \left( 2 c d - \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] - \\
 & \quad \left( 2 c e^2 \left( 3 c^2 d^2 + b \left( b - \sqrt{b^2 - 4 a c} \right) e^2 - c e \left( 3 b d - 2 \sqrt{b^2 - 4 a c} d + a e \right) \right) x \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \quad \left( \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^3 \right) + \\
 & \quad \frac{1}{a (b^2 - 4 a c) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^2 n} \\
 & \quad c \left( 4 a c^2 \left( e \left( a e (1 - 2 n) - \sqrt{b^2 - 4 a c} d (1 - n) \right) - c d^2 (1 - 2 n) \right) - \right. \\
 & \quad \quad b^2 c \left( e \left( a e (5 - 7 n) - 2 \sqrt{b^2 - 4 a c} d (1 - n) \right) - c d^2 (1 - n) \right) + \\
 & \quad \quad b c \left( c d \left( 4 a e (2 - 3 n) - \sqrt{b^2 - 4 a c} d (1 - n) \right) + 3 a \sqrt{b^2 - 4 a c} e^2 (1 - n) \right) + b^4 e^2 (1 - n) - \\
 & \quad \quad \left. b^3 e \left( 2 c d + \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] + \\
 & \quad \frac{2 e^4 (2 c d - b e) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d (c d^2 - b d e + a e^2)^3} + \\
 & \quad \frac{e^4 x \operatorname{Hypergeometric2F1} \left[ 2, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d^2 (c d^2 - b d e + a e^2)^2}
 \end{aligned}$$

Result (type 5, 16855 leaves):

$$\begin{aligned}
 & \left( -b^2 c^2 d^4 + 2 a c^3 d^4 + 2 b^3 c d^3 e - 6 a b c^2 d^3 e - b^4 d^2 e^2 + 4 a b^2 c d^2 e^2 - 2 a^2 c^2 d^2 e^2 - \right. \\
 & \quad \left. a^2 b^2 e^4 + 4 a^3 c e^4 + b^2 c^2 d^4 n - 4 a c^3 d^4 n - 2 b^3 c d^3 e n + 8 a b c^2 d^3 e n + b^4 d^2 e^2 n - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (2 a b^2 c d^2 e^2 n - 8 a^2 c^2 d^2 e^2 n - 2 a b^3 d e^3 n + 8 a^2 b c d e^3 n + a^2 b^2 e^4 n - 4 a^3 c e^4 n) x) / \\
 & \left( a^2 (-b^2 + 4 a c) d^2 (c d^2 - b d e + a e^2)^2 n \right) + \\
 & \left( b^2 c^2 d^4 - 2 a c^3 d^4 - 2 b^3 c d^3 e + 6 a b c^2 d^3 e + b^4 d^2 e^2 - 4 a b^2 c d^2 e^2 + 2 a^2 c^2 d^2 e^2 + \right. \\
 & \quad \left. a^2 b^2 e^4 - 4 a^3 c e^4 - b^2 c^2 d^4 n + 4 a c^3 d^4 n + 2 b^3 c d^3 e n - 8 a b c^2 d^3 e n - b^4 d^2 e^2 n + \right. \\
 & \quad \left. 2 a b^2 c d^2 e^2 n + 8 a^2 c^2 d^2 e^2 n + 2 a b^3 d e^3 n - 8 a^2 b c d e^3 n - a^2 b^2 e^4 n + 4 a^3 c e^4 n \right) x) / \\
 & \left( a^2 (-b^2 + 4 a c) d^2 (c d^2 - b d e + a e^2)^2 n \right) + \frac{e^4 x}{d (c d^2 - b d e + a e^2)^2 n (d + e x^n)} + \\
 & (-b^2 c^2 d^2 x + 2 a c^3 d^2 x + 2 b^3 c d e x - 6 a b c^2 d e x - b^4 e^2 x + 4 a b^2 c e^2 x - 2 a^2 c^2 e^2 x - \\
 & \quad b c^3 d^2 x^{1+n} + 2 b^2 c^2 d e x^{1+n} - 4 a c^3 d e x^{1+n} - b^3 c e^2 x^{1+n} + 3 a b c^2 e^2 x^{1+n}) / \\
 & \left( a (-b^2 + 4 a c) (c d^2 - b d e + a e^2)^2 n (a + b x^n + c x^{2 n}) \right) + \\
 & \left( e^4 (-c d^2 + b d e - a e^2 + 5 c d^2 n - 3 b d e n + a e^2 n) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right] \right) / \\
 & \left( d^2 (c d^2 - b d e + a e^2)^3 n \right) - \\
 & \left( b c^4 d^4 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) \right) / \\
 & \left( a (-b^2 + 4 a c) (c d^2 - b d e + a e^2)^3 \right) + \\
 & \left( 3 b^2 c^3 d^3 e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) \right) / \\
 & \left( a (-b^2 + 4 a c) (c d^2 - b d e + a e^2)^3 \right) -
 \end{aligned}$$

$$\left( 4 c^4 d^3 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$

$$\left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 \right) - \left( 3 b^3 c^2 d^2 e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \right.$$

$$\left. \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$

$$(a(-b^2+4 a c) (c d^2-b d e+a e^2)^3) +$$

$$\left( 6 b c^3 d^2 e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$



$$\left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 + \left( b^4 c d e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( a (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 + \left( 3b^2 c^2 d e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 - \left( 20ac^3 d e^3 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \right. \right.$$

$$\left. \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \Bigg/$$

$$\begin{aligned}
 & \left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 \right) - \left( 3b^3 c e^4 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right) \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \\
 & \left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 \right) + \left( 11abc^2 e^4 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \right. \\
 & \quad \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right) \right)^{-1/n} \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \\
 & \left( (-b^2 + 4ac) (cd^2 - bde + ae^2)^3 \right) + \left( bc^4 d^4 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right) \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/ \\
 & (a(-b^2 + 4ac) (cd^2 - bde + ae^2)^3 n) -
 \end{aligned}$$

$$\left( 3 b^2 c^3 d^3 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$

$$(a(-b^2+4 a c)(c d^2-b d e+a e^2)^3 n) +$$

$$\left( 4 c^4 d^3 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$

$$((-b^2+4 a c)(c d^2-b d e+a e^2)^3 n) +$$

$$\left( 3 b^3 c^2 d^2 e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) /$$

$$(a(-b^2+4 a c)(c d^2-b d e+a e^2)^3 n) -$$

$$\left( 6 b c^3 d^2 e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \Bigg/$$

$$\left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) -$$

$$\left( b^4 c d e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \Bigg/$$

$$\left( a (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) +$$

$$\left( b^2 c^2 d e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}}$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \Bigg/$$

$$\left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) +$$

$$\begin{aligned}
 & \left( 4 a c^3 d e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) + \left( b^3 c e^4 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) - \\
 & \left( 3 a b c^2 e^4 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) / \\
 & \left( (-b^2+4 a c) (c d^2-b d e+a e^2)^3 n \right) + \left( b^2 c^3 d^4 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)- \\
 & \left(4c^4d^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\right. \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)-\left(3b^3c^2d^3ex\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right/ \\
 & \left( \frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c} \right) + \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right/ \\
 & \left. \left( \frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c} \right) \right) \right/ \left( a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 \right) + \\
 & \left( 12bc^3d^3ex \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right/ \left( \frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c} \right) + \right. \\
 & \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right/ \left( \frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c} + \frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c} \right) \right) \right) \right/ \\
 & \left( \left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 \right) + \left( 3b^4cd^2e^2x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)- \\
 & \left(9b^2c^2d^2e^2x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)-\left(12ac^3d^2e^2x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)- \\
 & \left(b^5 d e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \\
 & \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right)\right/ \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)-\left(2 b^3 c d e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)+ \\
 & \left(24abc^2de^3x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\right. \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)+\left(3b^4e^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)- \\
 & \left(14ab^2ce^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \\
 & \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)+\left(8a^2c^2e^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3\right)- \\
 & \left(b^2c^3d^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3n\right)+\left(2c^4d^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)+ \\
 & \left(3 b^3 c^2 d^3 e x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right.\right. \\
 & \left.\left.\left.-\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right. \\
 & \left.\left.\left.-\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right)\right/ \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)-\left(8 b c^3 d^3 e x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)- \\
 & \left(3 b^4 c d^2 e^2 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right.\right. \\
 & \left.\left.\left.-\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+ \\
 & \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right. \\
 & \left.\left.\left.-\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right) \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)+\left(9 b^2 c^2 d^2 e^2 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)+ \\
 & \left(b^5 d e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right.\right.\right. \\
 & \left.\left.\left. -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)^2\right)+ \\
 & \left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n},\right. \\
 & \left.\left. -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)^2\right)\right)\right/ \\
 & \left(a\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right)-\left(2 b^3 c d e^3 x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
& \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
& \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
& \left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3n\right)- \\
& \left(4abc^2de^3x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right. \\
& \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\right. \\
& \left.\left(1-\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
& \left.\left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right/ \left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\right)\right/ \\
& \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3n\right)-\left(b^4e^4x\left(\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right.\right.
\end{aligned}$$



$$\begin{aligned}
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c}\right) + \left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/ \\
 & \left.\left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right)\right) \left/ \left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right) + \right. \\
 & \left(4ab^2ce^4x\left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \right. \right. \\
 & \left. \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right) \right/ \left(\frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c}\right) + \\
 & \left(1 - \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) \right/ \left(\frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c}\right) \right) \left/ \right. \\
 & \left.\left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3 n\right) - \left(2a^2c^2e^4x\left(\left(1 - \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right)\right.\right.\right.
 \end{aligned}$$

$$\left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/$$

$$\left(\frac{b\left(-b-\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b-\sqrt{b^2-4ac}\right)^2}{2c}\right)+\left(1-\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.$$

$$\left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right/$$

$$\left.\left(\frac{b\left(-b+\sqrt{b^2-4ac}\right)}{2c}+\frac{\left(-b+\sqrt{b^2-4ac}\right)^2}{2c}\right)\right)\left/\left(\left(-b^2+4ac\right)\left(cd^2-bde+ae^2\right)^3n\right)\right.$$

**Problem 80: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d+e x^n)^3}{(a+b x^n+c x^{2n})^3} dx$$

Optimal (type 5, 1707 leaves, 11 steps):

$$\left(x\left(b^2 c d^3-2 a c d\left(c d^2-3 a e^2\right)-\right.\right.$$

$$\left.\left.a b e\left(3 c d^2+a e^2\right)-\left(a b^2 e^3+2 a c e\left(3 c d^2-a e^2\right)-b c d\left(c d^2+3 a e^2\right)\right) x^n\right) /$$

$$\left(2 a c\left(b^2-4 a c\right) n\left(a+b x^n+c x^{2 n}\right)^2\right)+$$

$$\frac{e^2 x\left(3 b^2 c d-6 a c^2 d-b^3 e+a b c e+c\left(3 b c d-b^2 e-2 a c e\right) x^n\right)}{a c^2\left(b^2-4 a c\right) n\left(a+b x^n+c x^{2 n}\right)} -$$

$$\frac{1}{2 a^2 c^2\left(b^2-4 a c\right)^2 n^2\left(a+b x^n+c x^{2 n}\right)}$$

$$\times\left(a b^2 c^2 d\left(3 a e^2\left(1-9 n\right)-5 c d^2\left(1-3 n\right)\right)+4 a^2 c^3 d\left(c d^2-3 a e^2\right)\left(1-4 n\right)-2 a b^5 e^3 n+2 a^2 b c^2\right.$$

$$\left.e\left(3 c d^2\left(2-3 n\right)-5 a e^2 n\right)-3 a b^3 c e\left(c d^2-3 a e^2 n\right)+b^4 c d\left(c d^2\left(1-2 n\right)+6 a e^2 n\right)+\right.$$

$$\left.c\left(4 a^2 c^2 e\left(3 c d^2-a e^2\right)\left(1-3 n\right)-2 a b^4 e^3 n-2 a b c^2 d\left(c d^2\left(2-7 n\right)+3 a e^2 n\right)+\right.\right.$$

$$\left.\left.b^3 c d\left(c d^2\left(1-2 n\right)+6 a e^2 n\right)-a b^2 c e\left(3 c d^2-a e^2\left(1+2 n\right)\right)\right) x^n\right)+$$

$$\left(e^2\left(b c\left(2 a e\left(2-5 n\right)+3 \sqrt{b^2-4 a c} d\left(1-n\right)\right)-2 a c\left(6 c d\left(1-2 n\right)+\sqrt{b^2-4 a c} e\left(1-n\right)\right)-\right.\right.$$

$$\left.\left.b^3 e\left(1-n\right)+b^2\left(3 c d-\sqrt{b^2-4 a c} e\right)\left(1-n\right)\right)\right.$$

$$\left.\times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1+\frac{1}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}\right]\right) /$$

$$\begin{aligned}
 & \frac{\left( a c (b^2 - 4 a c) \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) n \right) +}{2 a^2 c (b^2 - 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) n^2} \\
 & \left( (1-n) (4 a^2 c^2 e (3 c d^2 - a e^2) (1-3 n) - 2 a b^4 e^3 n - 2 a b c^2 d (c d^2 (2-7 n) + 3 a e^2 n) + \right. \\
 & \quad \left. b^3 c d (c d^2 (1-2 n) + 6 a e^2 n) - a b^2 c e (3 c d^2 - a e^2 (1+2 n))) - \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left( 2 a b^5 e^3 (1-n) n - b^4 c d (1-n) (c d^2 (1-2 n) + 6 a e^2 n) - 8 a^2 c^3 d (c d^2 - 3 a e^2) \right. \\
 & \quad \left. (1-6 n+8 n^2) + 6 a b^2 c^2 d (c d^2 (1-4 n+3 n^2) - a e^2 (1-10 n+15 n^2)) - \right. \\
 & \quad \left. 4 a^2 b c^2 e (3 c d^2 (1-n-3 n^2) + a e^2 (1-11 n+19 n^2)) + \right. \\
 & \quad \left. a b^3 c e (3 c d^2 (1-n) + a e^2 (1-19 n+30 n^2)) \right) \\
 & \quad \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] + \\
 & \left( e^2 \left( b c \left( 2 a e (2-5 n) - 3 \sqrt{b^2 - 4 a c} d (1-n) \right) - 2 a c \left( 6 c d (1-2 n) - \sqrt{b^2 - 4 a c} e (1-n) \right) - \right. \right. \\
 & \quad \left. \left. b^3 e (1-n) + b^2 \left( 3 c d + \sqrt{b^2 - 4 a c} e \right) (1-n) \right) \right. \\
 & \quad \left. \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \frac{\left( a c (b^2 - 4 a c) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) n \right) +}{2 a^2 c (b^2 - 4 a c)^2 \left( b + \sqrt{b^2 - 4 a c} \right) n^2} \\
 & \left( (1-n) (4 a^2 c^2 e (3 c d^2 - a e^2) (1-3 n) - 2 a b^4 e^3 n - 2 a b c^2 d (c d^2 (2-7 n) + 3 a e^2 n) + \right. \\
 & \quad \left. b^3 c d (c d^2 (1-2 n) + 6 a e^2 n) - a b^2 c e (3 c d^2 - a e^2 (1+2 n))) + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left( 2 a b^5 e^3 (1-n) n - b^4 c d (1-n) (c d^2 (1-2 n) + 6 a e^2 n) - 8 a^2 c^3 d (c d^2 - 3 a e^2) \right. \\
 & \quad \left. (1-6 n+8 n^2) + 6 a b^2 c^2 d (c d^2 (1-4 n+3 n^2) - a e^2 (1-10 n+15 n^2)) - \right. \\
 & \quad \left. 4 a^2 b c^2 e (3 c d^2 (1-n-3 n^2) + a e^2 (1-11 n+19 n^2)) + \right. \\
 & \quad \left. a b^3 c e (3 c d^2 (1-n) + a e^2 (1-19 n+30 n^2)) \right) \\
 & \quad \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right]
 \end{aligned}$$

Result (type 5, 13018 leaves):

$$\begin{aligned}
 & \left( (-b^4 d^3 + 5 a b^2 c d^3 - 4 a^2 c^2 d^3 + 3 a b^3 d^2 e - 12 a^2 b c d^2 e - 3 a^2 b^2 d e^2 + 12 a^3 c d e^2 + 3 b^4 d^3 n - \right. \\
 & \quad \left. 21 a b^2 c d^3 n + 24 a^2 c^2 d^3 n - 3 a b^3 d^2 e n + 30 a^2 b c d^2 e n - 3 a^2 b^2 d e^2 n - 24 a^3 c d e^2 n + \right. \\
 & \quad \left. 6 a^3 b e^3 n - 2 b^4 d^3 n^2 + 16 a b^2 c d^3 n^2 - 32 a^2 c^2 d^3 n^2) x \right) / \left( 2 a^3 (-b^2 + 4 a c)^2 n^2 \right) + \\
 & \left( (b^4 d^3 - 5 a b^2 c d^3 + 4 a^2 c^2 d^3 - 3 a b^3 d^2 e + 12 a^2 b c d^2 e + 3 a^2 b^2 d e^2 - 12 a^3 c d e^2 - 3 b^4 d^3 n + \right. \\
 & \quad \left. 21 a b^2 c d^3 n - 24 a^2 c^2 d^3 n + 3 a b^3 d^2 e n - 30 a^2 b c d^2 e n + 3 a^2 b^2 d e^2 n + 24 a^3 c d e^2 n - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{6 a^3 b e^3 n+2 b^4 d^3 n^2-16 a b^2 c d^3 n^2+32 a^2 c^2 d^3 n^2) x}{\left(2 a^3\left(-b^2+4 a c\right)^2 n^2\right)-} \\
 & \left(x\left(b^2 c d^3-2 a c^2 d^3-3 a b c d^2 e+6 a^2 c d e^2-a^2 b e^3+b c^2 d^3 x^n-\right.\right. \\
 & \left.\left.6 a c^2 d^2 e x^n+3 a b c d e^2 x^n-a b^2 e^3 x^n+2 a^2 c e^3 x^n\right)\right) / \\
 & \left(2 a c\left(-b^2+4 a c\right) n\left(a+b x^n+c x^{2 n}\right)^2\right)+\frac{1}{2 a^2 c\left(-b^2+4 a c\right)^2 n^2\left(a+b x^n+c x^{2 n}\right)} \\
 & \left(-b^4 c d^3 x+5 a b^2 c^2 d^3 x-4 a^2 c^3 d^3 x+3 a b^3 c d^2 e x-12 a^2 b c^2 d^2 e x-3 a^2 b^2 c d e^2 x+\right. \\
 & \left.12 a^3 c^2 d e^2 x+2 b^4 c d^3 n x-15 a b^2 c^2 d^3 n x+16 a^2 c^3 d^3 n x+18 a^2 b c^2 d^2 e n x-\right. \\
 & \left.9 a^2 b^2 c d e^2 n x+a^2 b^3 e^3 n x+2 a^3 b c e^3 n x-b^3 c^2 d^3 x^{1+n}+4 a b c^3 d^3 x^{1+n}+3 a b^2 c^2 d^2 e x^{1+n}-\right. \\
 & \left.12 a^2 c^3 d^2 e x^{1+n}-a^2 b^2 c e^3 x^{1+n}+4 a^3 c^2 e^3 x^{1+n}+2 b^3 c^2 d^3 n x^{1+n}-14 a b c^3 d^3 n x^{1+n}+\right. \\
 & \left.36 a^2 c^3 d^2 e n x^{1+n}-18 a^2 b c^2 d e^2 n x^{1+n}+2 a^2 b^2 c e^3 n x^{1+n}+4 a^3 c^2 e^3 n x^{1+n}\right)+ \\
 & \frac{1}{a^2\left(-b^2+4 a c\right)^2} b^3 c d^3 x^{1+n}\left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4 a c}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n}\right)^{-1 / n}\right. \\
 & \left.\text{Hypergeometric2F1}\left[-\frac{1}{n},-\frac{1}{n}, \frac{-1+n}{n},-\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right]+\frac{1}{\sqrt{b^2-4 a c}}\right. \\
 & \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n}\right)^{-1 / n}\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n},-\frac{1}{n}, \frac{-1+n}{n},-\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right]\right)- \\
 & \frac{1}{a\left(-b^2+4 a c\right)^2} 7 b c^2 d^3 x^{1+n}\left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4 a c}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n}\right)^{-1 / n}\right. \\
 & \left.\text{Hypergeometric2F1}\left[-\frac{1}{n},-\frac{1}{n}, \frac{-1+n}{n},-\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right]+\frac{1}{\sqrt{b^2-4 a c}}\right. \\
 & \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n}\right)^{-1 / n}\right. \\
 & \left.\left.\text{Hypergeometric2F1}\left[-\frac{1}{n},-\frac{1}{n}, \frac{-1+n}{n},-\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right]\right)+ \\
 & \frac{1}{\left(-b^2+4 a c\right)^2} 18 c^2 d^2 e x^{1+n}\left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}}\left(-\frac{1}{\sqrt{b^2-4 a c}}\left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n}\right)^{-1 / n}\right. \\
 & \left.\text{Hypergeometric2F1}\left[-\frac{1}{n},-\frac{1}{n}, \frac{-1+n}{n},-\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right]+\frac{1}{\sqrt{b^2-4 a c}}\right.
 \end{aligned}$$

$$\left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] -$$

$$\frac{1}{(-b^2+4ac)^2} 9 b c d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\frac{1}{(-b^2+4ac)^2} b^2 e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\frac{1}{(-b^2+4ac)^2} 2 a c e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\left( b^3 c d^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\ \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\ \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) / \\ \left( 2 a^2 (-b^2+4ac)^2 n^2 \right) - \left( 2 b c^2 d^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\ \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\ \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) / \\ \left( a (-b^2+4ac)^2 n^2 \right) - \left( 3 b^2 c d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\ \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\ \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) / \\ \left( 2 a (-b^2+4ac)^2 n^2 \right) + \frac{1}{(-b^2+4ac)^2 n^2} 6 c^2 d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\begin{aligned}
 & \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) + \\
 & \left( b^2 e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right. \\
 & \quad \left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \right) \Bigg/ \\
 & \left( 2(-b^2+4ac)^2 n^2 \right) - \frac{1}{(-b^2+4ac)^2 n^2} 2ac e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \\
 & \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) -
 \end{aligned}$$

$$\left( 3 b^3 c d^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}} \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right)$$

$$\left( 2 a^2 (-b^2+4 a c)^2 n \right) + \frac{1}{a (-b^2+4 a c)^2 n} 9 b c^2 d^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}} \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right) +$$

$$\left( 3 b^2 c d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4 a c}} \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c\left(-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)}\right] \right) \right)$$

$$\left( 2 a (-b^2+4 a c)^2 n \right) - \frac{1}{(-b^2+4 a c)^2 n} 24 c^2 d^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$



$$\begin{aligned}
 & \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) + \\
 & \frac{1}{(-b^2+4ac)^2 n} 9 b c d e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) - \\
 & \frac{1}{2(-b^2+4ac)^2 n} 3 b^2 e^3 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) - \\
 & \frac{1}{a^2(-b^2+4ac)^2} b^4 d^3 x
 \end{aligned}$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b + \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) + \frac{1}{a \left( -b^2 + 4 a c \right)^2} 8 b^2 c d^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b + \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) - \frac{1}{\left( -b^2 + 4 a c \right)^2} 16 c^2 d^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b + \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) -$$

$$\left( b^4 d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b + \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b + \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) \right) /$$

$$\left( 2 a^2 \left( -b^2 + 4 a c \right)^2 n^2 \right) + \left( 5 b^2 c d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right.$$

$$\left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4 a c} \right)}{2 c} + \frac{\left( -b - \sqrt{b^2 - 4 a c} \right)^2}{2 c} \right) \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \right/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \right) \right/$$

$$(2a(-b^2 + 4ac)^2 n^2) - \frac{1}{(-b^2 + 4ac)^2 n^2} 2c^2 d^3 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 3b^3 d^2 e x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \right) \right) \right/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \right/$$

$$(2 a (-b^2 + 4 a c)^2 n^2) - \frac{1}{(-b^2 + 4 a c)^2 n^2} 6 b c d^2 e x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) -$$

$$\left( 3 b^2 d e^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \right. \\ \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) / \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\ \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right) / \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) /$$

$$(2 (-b^2 + 4 a c)^2 n^2) + \frac{1}{(-b^2 + 4 a c)^2 n^2} 6 a c d e^2 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\ \left. \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right. \\ \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\ \left. \left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) \right) + \\ \left( 3 b^4 d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\ \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right. \\ \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\ \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) \right) \right) / \\ \left( 2 a^2 \left( -b^2 + 4 a c \right)^2 n \right) - \left( 21 b^2 c d^3 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \\ \left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right. \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\ \left. \left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) \Bigg) / \\ (2a(-b^2+4ac)^2n) + \frac{1}{(-b^2+4ac)^2n} 12c^2d^3$$

x

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\ \left. \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\ \left. \left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) \right) -$$

$$\left( 3b^3d^2ex \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\ \left. \left. - \frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \right) \right/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \right) \right/$$

$$(2a(-b^2 + 4ac)^2 n) + \frac{1}{(-b^2 + 4ac)^2 n} 15bcd^2$$

e  
x

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \right/$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) - \frac{1}{2(-b^2 + 4ac)^2 n} 3b^2 d e^2 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right) \right/$$

$$\left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)} \right] \right) \right/$$

$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) - \frac{1}{(-b^2 + 4ac)^2 n} 12ac d e^2 x$$



$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \frac{1}{(-b^2 + 4ac)^2 n} 3 a b e^3 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right)$$

**Problem 81: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d + e x^n)^2}{(a + b x^n + c x^{2n})^3} dx$$

Optimal (type 5, 1191 leaves, 11 steps):

$$\begin{aligned}
 & \frac{x \left( b^2 d^2 - 2 a b d e - 2 a \left( c d^2 - a e^2 \right) + \left( b c d^2 - 4 a c d e + a b e^2 \right) x^n \right)}{2 a \left( b^2 - 4 a c \right) n \left( a + b x^n + c x^{2 n} \right)^2} + \\
 & \frac{e^2 x \left( b^2 - 2 a c + b c x^n \right)}{a c \left( b^2 - 4 a c \right) n \left( a + b x^n + c x^{2 n} \right)} + \\
 & \frac{\left( x \left( 2 a b^3 c d e - a b^2 c \left( a e^2 \left( 1 - 9 n \right) - 5 c d^2 \left( 1 - 3 n \right) \right) - 4 a^2 c^2 \left( c d^2 - a e^2 \right) \left( 1 - 4 n \right) - \right. \right.}{4 a^2 b c^2 d e \left( 2 - 3 n \right) - b^4 \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) + c \left( 2 a b^2 c d e - 8 a^2 c^2 d e \left( 1 - 3 n \right) + \right.} \\
 & \quad \left. \left. 2 a b c \left( c d^2 \left( 2 - 7 n \right) + a e^2 n \right) - b^3 \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) \right) x^n \right) /}{\left( 2 a^2 c \left( b^2 - 4 a c \right)^2 n^2 \left( a + b x^n + c x^{2 n} \right) - \left( e^2 \left( 4 a c \left( 1 - 2 n \right) - b^2 \left( 1 - n \right) - b \sqrt{b^2 - 4 a c} \left( 1 - n \right) \right) \right)} \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) /} \\
 & \left( a \left( b^2 - 4 a c \right) \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) n \right) - \\
 & \left( \left( \left( 1 - n \right) \left( 2 a b^2 c d e - 8 a^2 c^2 d e \left( 1 - 3 n \right) + \right. \right. \right. \\
 & \quad \left. \left. 2 a b c \left( c d^2 \left( 2 - 7 n \right) + a e^2 n \right) - b^3 \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) \right) + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left. \left( 2 a b^3 c d e \left( 1 - n \right) - b^4 \left( 1 - n \right) \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) - 8 a^2 b c^2 d e \left( 1 - n - 3 n^2 \right) - \right. \right. \\
 & \quad \left. \left. 8 a^2 c^2 \left( c d^2 - a e^2 \right) \left( 1 - 6 n + 8 n^2 \right) + 2 a b^2 c \left( 3 c d^2 \left( 1 - 4 n + 3 n^2 \right) - a e^2 \left( 1 - 10 n + 15 n^2 \right) \right) \right) \right) \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) /} \\
 & \left( 2 a^2 \left( b^2 - 4 a c \right)^2 \left( b - \sqrt{b^2 - 4 a c} \right) n^2 \right) - \\
 & \left( e^2 \left( 4 a c \left( 1 - 2 n \right) - b^2 \left( 1 - n \right) + b \sqrt{b^2 - 4 a c} \left( 1 - n \right) \right) x \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) /} \\
 & \left( a \left( b^2 - 4 a c \right) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) n \right) - \\
 & \left( \left( \left( 1 - n \right) \left( 2 a b^2 c d e - 8 a^2 c^2 d e \left( 1 - 3 n \right) + 2 a b c \left( c d^2 \left( 2 - 7 n \right) + a e^2 n \right) - \right. \right. \right. \\
 & \quad \left. \left. b^3 \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) \right) - \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left. \left( 2 a b^3 c d e \left( 1 - n \right) - b^4 \left( 1 - n \right) \left( c d^2 \left( 1 - 2 n \right) + 2 a e^2 n \right) - 8 a^2 b c^2 d e \left( 1 - n - 3 n^2 \right) - \right. \right. \\
 & \quad \left. \left. 8 a^2 c^2 \left( c d^2 - a e^2 \right) \left( 1 - 6 n + 8 n^2 \right) + 2 a b^2 c \left( 3 c d^2 \left( 1 - 4 n + 3 n^2 \right) - a e^2 \left( 1 - 10 n + 15 n^2 \right) \right) \right) \right) \\
 & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \left( 2 a^2 \left( b^2 - 4 a c \right)^2 \left( b + \sqrt{b^2 - 4 a c} \right) n^2 \right)
 \end{aligned}$$

Result (type 5, 10910 leaves):

$$\begin{aligned}
 & \left( -b^4 d^2 + 5 a b^2 c d^2 - 4 a^2 c^2 d^2 + 2 a b^3 d e - 8 a^2 b c d e - a^2 b^2 e^2 + 4 a^3 c e^2 + \right. \\
 & \quad \left. 3 b^4 d^2 n - 21 a b^2 c d^2 n + 24 a^2 c^2 d^2 n - 2 a b^3 d e n + 20 a^2 b c d e n - a^2 b^2 e^2 n - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (b^4 d^2 - 5 a b^2 c d^2 + 4 a^2 c^2 d^2 - 2 a b^3 d e + 8 a^2 b c d e + a^2 b^2 e^2 - 4 a^3 c e^2 - 3 b^4 d^2 n + \right. \\
 & \quad \left. 21 a b^2 c d^2 n - 24 a^2 c^2 d^2 n + 2 a b^3 d e n - 20 a^2 b c d e n + a^2 b^2 e^2 n + 8 a^3 c e^2 n + \right. \\
 & \quad \left. 2 b^4 d^2 n^2 - 16 a b^2 c d^2 n^2 + 32 a^2 c^2 d^2 n^2) x \right) / \left( 2 a^3 (-b^2 + 4 a c)^2 n^2 \right) + \\
 & \frac{x (b^2 d^2 - 2 a c d^2 - 2 a b d e + 2 a^2 e^2 + b c d^2 x^n - 4 a c d e x^n + a b e^2 x^n)}{2 a (-b^2 + 4 a c) n (a + b x^n + c x^{2n})^2} + \\
 & \frac{1}{2 a^2 (-b^2 + 4 a c)^2 n^2 (a + b x^n + c x^{2n})} \\
 & \left( -b^4 d^2 x + 5 a b^2 c d^2 x - 4 a^2 c^2 d^2 x + 2 a b^3 d e x - 8 a^2 b c d e x - a^2 b^2 e^2 x + \right. \\
 & \quad \left. 4 a^3 c e^2 x + 2 b^4 d^2 n x - 15 a b^2 c d^2 n x + 16 a^2 c^2 d^2 n x + 12 a^2 b c d e n x - \right. \\
 & \quad \left. 3 a^2 b^2 e^2 n x - b^3 c d^2 x^{1+n} + 4 a b c^2 d^2 x^{1+n} + 2 a b^2 c d e x^{1+n} - 8 a^2 c^2 d e x^{1+n} + \right. \\
 & \quad \left. 2 b^3 c d^2 n x^{1+n} - 14 a b c^2 d^2 n x^{1+n} + 24 a^2 c^2 d e n x^{1+n} - 6 a^2 b c e^2 n x^{1+n} \right) + \\
 & \frac{1}{a^2 (-b^2 + 4 a c)^2} b^3 c d^2 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) - \\
 & \frac{1}{a (-b^2 + 4 a c)^2} 7 b c^2 d^2 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2 - 4 a c}} \right. \\
 & \quad \left. \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c \left( -\frac{-b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)} \right] \right) + \\
 & \frac{1}{(-b^2 + 4 a c)^2} 12 c^2 d e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] - \\
 & \frac{1}{(-b^2+4ac)^2} 3bc e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right. \\
 & \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) + \\
 & \left(b^3 c d^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right.\right. \\
 & \left. \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right)\right) \Big/ \\
 & (2a^2(-b^2+4ac)^2 n^2) - \left(2bc^2 d^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right.\right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right.\right.
 \end{aligned}$$

$$\left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \Bigg) \Bigg/$$

$$(a(-b^2+4ac)^2 n^2) - \left( b^2 c d e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \Bigg) \Bigg/$$

$$(a(-b^2+4ac)^2 n^2) + \frac{1}{(-b^2+4ac)^2 n^2} 4 c^2 d e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) -$$

$$\left( 3 b^3 c d^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right. \right.$$

$$\left( \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \Bigg/$$

$$(2 a^2 (-b^2 + 4 a c)^2 n) + \frac{1}{a (-b^2 + 4 a c)^2 n} 9 b c^2 d^2 x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}}$$

$$\left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) +$$

$$\frac{1}{a (-b^2 + 4 a c)^2 n} b^2 c d e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) -$$

$$\frac{1}{(-b^2 + 4 a c)^2 n} 16 c^2 d e x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\begin{aligned}
 & \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \\
 & \frac{1}{(-b^2+4ac)^2 n} 3bc e^2 x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ \right. \right. \\
 & \quad \left. \left. -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] - \frac{1}{a^2 (-b^2+4ac)^2} b^4 d^2 x \right. \\
 & \quad \left. \left( \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \quad \left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right. \\
 & \quad \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \quad \left. \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{a(-b^2+4ac)^2} 8b^2 c d^2 x \right. \\
 & \quad \left. \left( \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \quad \left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.
 \end{aligned}$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) - \frac{1}{\left( -b^2+4ac \right)^2} 16 c^2 d^2 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) -$$

$$\left( b^4 d^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) /$$



$$\begin{aligned}
 & \left( 2 a^2 (-b^2 + 4 a c)^2 n^2 \right) + \left( 5 b^2 c d^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4 a c} \right)}{2 c} + \frac{\left( -b-\sqrt{b^2-4 a c} \right)^2}{2 c} \right)^2 \right) + \\
 & \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4 a c} \right)}{2 c} + \frac{\left( -b+\sqrt{b^2-4 a c} \right)^2}{2 c} \right)^2 \right) / \\
 & \left( 2 a \left( -b^2 + 4 a c \right)^2 n^2 \right) - \frac{1}{\left( -b^2 + 4 a c \right)^2 n^2} 2 c^2 d^2 x \\
 & \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c} + x^n \right)} \right] \right) / \right. \\
 & \left. \left( \frac{b \left( -b-\sqrt{b^2-4 a c} \right)}{2 c} + \frac{\left( -b-\sqrt{b^2-4 a c} \right)^2}{2 c} \right)^2 \right) + \\
 & \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c} + x^n \right)} \right] \right) / \\
 & \left. \left( \frac{b \left( -b+\sqrt{b^2-4 a c} \right)}{2 c} + \frac{\left( -b+\sqrt{b^2-4 a c} \right)^2}{2 c} \right)^2 \right) + \\
 & \left( b^3 d e x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \left. \frac{-b-\sqrt{b^2-4ac}}{2c} \right) \right] \right/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right. \right. \\
 \left. \left. \left. \left. \left. \left. 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 \left. \left. \left. \left. \left. \left. \frac{-b+\sqrt{b^2-4ac}}{2c} \right) \right] \right) \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \left/ \right. \\
 \left( a(-b^2+4ac)^2 n^2 - \frac{1}{(-b^2+4ac)^2 n^2} 4bc d e x \right) \\
 \left( \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \right/ \right. \\
 \left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right) \right. \\
 \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) \left/ \right. \\
 \left. \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) - \\
 \left( b^2 e^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right. \right. \right. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 \left. \left. \left. \left. \left. \left. \frac{-b-\sqrt{b^2-4ac}}{2c} \right) \right] \right) \right/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) \right) \right) \right.$$

$$\begin{aligned}
 & \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \quad \left. \left. - \frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \Bigg) / \\
 & \left( 2 \left( -b^2+4ac \right)^2 n^2 \right) + \frac{1}{\left( -b^2+4ac \right)^2 n^2} 2ac e^2 x \\
 & \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \quad \left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right. \\
 & \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right. \\
 & \quad \left. \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) + \\
 & \left( 3b^4 d^2 x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \quad \left. \left. - \frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right. \\
 & \quad \left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \left/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \Bigg/ \\
 & (2a^2(-b^2 + 4ac)^2 n) - \left( 21b^2 c d^2 x \left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \\
 & \left. \left. \left. \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \left/ \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) \right) + \right. \\
 & \left. \left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \left/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \Bigg/ \\
 & (2a(-b^2 + 4ac)^2 n) + \frac{1}{(-b^2 + 4ac)^2 n} 12c^2 d^2 \\
 & x \\
 & \left( \left( \left( 1 - \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \left( -\frac{-b - \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \right) \right/ \\
 & \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \\
 & \left( 1 - \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b + \sqrt{b^2 - 4ac}}{2c} \left( -\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n \right) \right] \Bigg/ \\
 & \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \Bigg) - \frac{1}{a(-b^2 + 4ac)^2 n} b^3 d e x
 \end{aligned}$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{(-b^2+4ac)^2 n} 10 b c d e x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) - \frac{1}{2(-b^2+4ac)^2 n} b^2 e^2 x$$

$$\left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right) - \frac{1}{\left( -b^2 + 4ac \right)^2 n} 4ac e^2 x$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b \left( -b - \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b - \sqrt{b^2 - 4ac} \right)^2}{2c} \right) + \right.$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b + \sqrt{b^2 - 4ac} \right)}{2c} + \frac{\left( -b + \sqrt{b^2 - 4ac} \right)^2}{2c} \right)$$

**Problem 82: Result more than twice size of optimal antiderivative.**

$$\int \frac{d + e x^n}{(a + b x^n + c x^{2n})^3} dx$$

Optimal (type 5, 713 leaves, 5 steps):

$$\begin{aligned}
 & \frac{x (b^2 d - 2 a c d - a b e + c (b d - 2 a e) x^n)}{2 a (b^2 - 4 a c) n (a + b x^n + c x^{2n})^2} + \\
 & \left( x (a b^3 e - 4 a^2 c^2 d (1 - 4 n) + 5 a b^2 c d (1 - 3 n) - 2 a^2 b c e (2 - 3 n) - \right. \\
 & \quad \left. b^4 d (1 - 2 n) + c (a b^2 e + 2 a b c d (2 - 7 n) - 4 a^2 c e (1 - 3 n) - b^3 d (1 - 2 n)) x^n \right) / \\
 & \left( 2 a^2 (b^2 - 4 a c)^2 n^2 (a + b x^n + c x^{2n}) \right) + \\
 & \left( c (a b^2 (\sqrt{b^2 - 4 a c} e + 6 c d (1 - 3 n)) (1 - n) + b^3 (a e - \sqrt{b^2 - 4 a c} d (1 - 2 n)) (1 - n) - \right. \\
 & \quad \left. b^4 d (1 - 3 n + 2 n^2) - 2 a b c (2 a e (1 - n - 3 n^2) - \sqrt{b^2 - 4 a c} d (2 - 9 n + 7 n^2)) - \right. \\
 & \quad \left. 4 a^2 c (\sqrt{b^2 - 4 a c} e (1 - 4 n + 3 n^2) + 2 c d (1 - 6 n + 8 n^2)) \right) \\
 & \quad \times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right] / \\
 & \left( 2 a^2 (b^2 - 4 a c)^2 (b^2 - 4 a c - b \sqrt{b^2 - 4 a c}) n^2 \right) - \\
 & \left( c (a b^2 (\sqrt{b^2 - 4 a c} e - 6 c d (1 - 3 n)) (1 - n) - b^3 (a e + \sqrt{b^2 - 4 a c} d (1 - 2 n)) (1 - n) + \right. \\
 & \quad \left. b^4 d (1 - 3 n + 2 n^2) + 2 a b c (2 a e (1 - n - 3 n^2) + \sqrt{b^2 - 4 a c} d (2 - 9 n + 7 n^2)) - \right. \\
 & \quad \left. 4 a^2 c (\sqrt{b^2 - 4 a c} e (1 - 4 n + 3 n^2) - 2 c d (1 - 6 n + 8 n^2)) \right) \\
 & \quad \times \text{Hypergeometric2F1}\left[1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] / \\
 & \left( 2 a^2 (b^2 - 4 a c)^2 (b^2 - 4 a c + b \sqrt{b^2 - 4 a c}) n^2 \right)
 \end{aligned}$$

Result (type 5, 8593 leaves):

$$\begin{aligned}
 & \left( (-b^4 d + 5 a b^2 c d - 4 a^2 c^2 d + a b^3 e - 4 a^2 b c e + 3 b^4 d n - 21 a b^2 c d n + 24 a^2 c^2 d n - a b^3 e n + \right. \\
 & \quad \left. 10 a^2 b c e n - 2 b^4 d n^2 + 16 a b^2 c d n^2 - 32 a^2 c^2 d n^2) x \right) / \left( 2 a^3 (-b^2 + 4 a c)^2 n^2 \right) + \\
 & \left( (b^4 d - 5 a b^2 c d + 4 a^2 c^2 d - a b^3 e + 4 a^2 b c e - 3 b^4 d n + 21 a b^2 c d n - 24 a^2 c^2 d n + \right. \\
 & \quad \left. a b^3 e n - 10 a^2 b c e n + 2 b^4 d n^2 - 16 a b^2 c d n^2 + 32 a^2 c^2 d n^2) x \right) / \\
 & \left( 2 a^3 (-b^2 + 4 a c)^2 n^2 \right) + \frac{x (-b^2 d + 2 a c d + a b e - b c d x^n + 2 a c e x^n)}{2 a (-b^2 + 4 a c) n (a + b x^n + c x^{2n})^2} + \\
 & \left( -b^4 d x + 5 a b^2 c d x - 4 a^2 c^2 d x + a b^3 e x - 4 a^2 b c e x + 2 b^4 d n x - 15 a b^2 c d n x + \right. \\
 & \quad \left. 16 a^2 c^2 d n x + 6 a^2 b c e n x - b^3 c d x^{1+n} + 4 a b c^2 d x^{1+n} + a b^2 c e x^{1+n} - \right. \\
 & \quad \left. 4 a^2 c^2 e x^{1+n} + 2 b^3 c d n x^{1+n} - 14 a b c^2 d n x^{1+n} + 12 a^2 c^2 e n x^{1+n} \right) / \\
 & \left( 2 a^2 (-b^2 + 4 a c)^2 n^2 (a + b x^n + c x^{2n}) \right) + \frac{1}{a^2 (-b^2 + 4 a c)^2} \\
 & b^3 c d x^{1+n} (x^n)^{\frac{1}{n} - \frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2 - 4 a c}} \left( \frac{x^n}{-\frac{-b - \sqrt{b^2 - 4 a c}}{2 c} + x^n} \right)^{-1/n} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \\
 & \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] - \\
 & \frac{1}{a(-b^2+4ac)^2} 7bc^2 dx^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right. \\
 & \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) + \\
 & \frac{1}{(-b^2+4ac)^2} 6c^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \\
 & \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right. \\
 & \left.\left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right]\right) + \\
 & \left(b^3 c d x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n}\right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}}\right. \right.
 \end{aligned}$$



$$\left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n \right)} \right] \right) \Bigg/$$

$$\left( 2 a^2 (-b^2+4 a c)^2 n^2 \right) - \left( 2 b c^2 d x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( a (-b^2+4 a c)^2 n^2 \right) - \left( b^2 c e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}} \left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right. \right.$$

$$\left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right. \right.$$

$$\left. \left. \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b+\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] \right) \right) \Bigg/$$

$$\left( 2 a (-b^2+4 a c)^2 n^2 \right) + \frac{1}{(-b^2+4 a c)^2 n^2} 2 c^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\left( -\frac{1}{\sqrt{b^2-4 a c}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n} \right)^{-1/n} \right.$$

$$\left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4 a c}}{2 c \left( -\frac{-b-\sqrt{b^2-4 a c}}{2 c}+x^n \right)} \right] + \frac{1}{\sqrt{b^2-4 a c}} \right)$$

$$\left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n} \right)^{-1/n} \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] -$$

$$\left( 3 b^3 c d x^{1+n} \left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left. \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) \right) /$$

$$\left( 2 a^2 \left(-b^2+4 a c\right)^2 n\right) + \frac{1}{a\left(-b^2+4 a c\right)^2 n} 9 b c^2 d x^{1+n} \left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left. \left(\frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c\left(-\frac{-b+\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] \right) +$$

$$\left( b^2 c e x^{1+n} \left(x^n\right)^{\frac{1}{n}-\frac{1+n}{n}} \left(-\frac{1}{\sqrt{b^2-4ac}} \left(\frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n}\right)^{-1/n} \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c\left(-\frac{-b-\sqrt{b^2-4ac}}{2c}+x^n\right)}\right] + \frac{1}{\sqrt{b^2-4ac}} \right.$$

$$\left( \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$(2a(-b^2+4ac)^2n) - \frac{1}{(-b^2+4ac)^2n} 8c^2 e x^{1+n} (x^n)^{\frac{1}{n}-\frac{1+n}{n}}$$

$$\left( -\frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] + \frac{1}{\sqrt{b^2-4ac}} \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \right.$$

$$\left. \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] - \frac{1}{a^2(-b^2+4ac)^2} b^4 dx \right)$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) + \frac{1}{a(-b^2+4ac)^2} 8b^2 c dx$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) +$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) - \frac{1}{(-b^2+4ac)^2} 16c^2 dx$$

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) -$$

$$\left( b^4 dx \left( \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \right] \right/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \right) \Bigg/ \\
 & \left( 2a^2(-b^2+4ac)^2n^2 \right) + \left( 5b^2cdx \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \\
 & \left. \left. \left. \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \right) \right/ \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \right. \\
 & \left. \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c} \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \right) \right) \Bigg/ \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) \Bigg) \Bigg/ \\
 & \left( 2a(-b^2+4ac)^2n^2 \right) - \frac{1}{(-b^2+4ac)^2n^2} 2c^2dx \\
 & \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c} \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \right) \Bigg/ \\
 & \left( \frac{b(-b-\sqrt{b^2-4ac})}{2c} + \frac{(-b-\sqrt{b^2-4ac})^2}{2c} \right) + \\
 & \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c} \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right) \right] \Bigg/ \\
 & \left( \frac{b(-b+\sqrt{b^2-4ac})}{2c} + \frac{(-b+\sqrt{b^2-4ac})^2}{2c} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( b^3 e x \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right. \\
 & \quad \left. \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \quad \left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) / \\
 & \quad \left( 2a \left( -b^2 + 4ac \right)^2 n^2 \right) - \frac{1}{\left( -b^2 + 4ac \right)^2 n^2} 2bcex \\
 & \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \\
 & \quad \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \\
 & \quad \left( 1 - \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] / \\
 & \quad \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) + \\
 & \left( 3b^4 dx \left( \left( 1 - \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. - \frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] \Bigg/ \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) + \\
 & \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \\
 & \left. \left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \Bigg/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \Bigg/ \\
 & (2a^2(-b^2 + 4ac)^2n) - \left( 21b^2cdx \left( \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] \Bigg/ \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) \right) + \right. \\
 & \left. \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right. \\
 & \left. \left. \left. - \frac{-b + \sqrt{b^2 - 4ac}}{2c} \right] \Bigg/ \left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right) \right) \right) \Bigg/ \\
 & (2a(-b^2 + 4ac)^2n) + \frac{1}{(-b^2 + 4ac)^2n} 12c^2
 \end{aligned}$$

d  
x

$$\begin{aligned}
 & \left( \left( 1 - \left( \frac{x^n}{-\frac{-b + \sqrt{b^2 - 4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b - \sqrt{b^2 - 4ac}}{2c} \right] \Bigg/ \right. \\
 & \left. \left( \frac{b(-b - \sqrt{b^2 - 4ac})}{2c} + \frac{(-b - \sqrt{b^2 - 4ac})^2}{2c} \right) \right) +
 \end{aligned}$$

$$\left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) /$$

$$\left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) -$$

$$\left( b^3 e x \left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, \right. \right. \right.$$

$$\left. \left. \left. -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \left( \frac{b \left( -b+\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b+\sqrt{b^2-4ac} \right)^2}{2c} \right) \right) /$$

$$\left( 2 a \left( -b^2+4 a c \right)^2 n \right) + \frac{1}{\left( -b^2+4 a c \right)^2 n} 5 b c$$

e  
x

$$\left( \left( 1 - \left( \frac{x^n}{-\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b-\sqrt{b^2-4ac}}{2c \left( -\frac{-b-\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$

$$\left. \left( \frac{b \left( -b-\sqrt{b^2-4ac} \right)}{2c} + \frac{\left( -b-\sqrt{b^2-4ac} \right)^2}{2c} \right) + \right.$$

$$\left. \left( 1 - \left( \frac{x^n}{-\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n} \right)^{-1/n} \text{Hypergeometric2F1} \left[ -\frac{1}{n}, -\frac{1}{n}, \frac{-1+n}{n}, -\frac{-b+\sqrt{b^2-4ac}}{2c \left( -\frac{-b+\sqrt{b^2-4ac}}{2c} + x^n \right)} \right] \right) / \right.$$



$$\left( \frac{b(-b + \sqrt{b^2 - 4ac})}{2c} + \frac{(-b + \sqrt{b^2 - 4ac})^2}{2c} \right)$$

### Problem 83: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(d + e x^n) (a + b x^n + c x^{2n})^3} dx$$

Optimal (type 5, 1708 leaves, 15 steps):

$$\begin{aligned} & \frac{x (b^2 c d - 2 a c^2 d - b^3 e + 3 a b c e + c (b c d - b^2 e + 2 a c e) x^n)}{2 a (b^2 - 4 a c) (c d^2 - b d e + a e^2) n (a + b x^n + c x^{2n})^2} + \\ & \frac{e^2 x (b^2 c d - 2 a c^2 d - b^3 e + 3 a b c e + c (b c d - b^2 e + 2 a c e) x^n)}{a (b^2 - 4 a c) (c d^2 - b d e + a e^2)^2 n (a + b x^n + c x^{2n})} + \\ & \left( x (2 a^2 b c^2 e (4 - 11 n) - 3 a b^3 c e (2 - 5 n) - 4 a^2 c^3 d (1 - 4 n) + \right. \\ & \quad \left. 5 a b^2 c^2 d (1 - 3 n) - b^4 c d (1 - 2 n) + b^5 (e - 2 e n) - c (a b^2 c e (5 - 14 n) - \right. \\ & \quad \left. 2 a b c^2 d (2 - 7 n) - 4 a^2 c^2 e (1 - 3 n) + b^3 c d (1 - 2 n) - b^4 e (1 - 2 n)) x^n \right) / \\ & \left( 2 a^2 (b^2 - 4 a c)^2 (c d^2 - b d e + a e^2) n^2 (a + b x^n + c x^{2n}) \right) - \\ & \left( c e^4 \left( 2 c d - (b + \sqrt{b^2 - 4 a c}) e \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left( (b^2 - 4 a c - b \sqrt{b^2 - 4 a c}) (c d^2 - b d e + a e^2)^3 \right) + \\ & \left( c e^2 \left( b c \left( 2 a e (2 - 3 n) + \sqrt{b^2 - 4 a c} d (1 - n) \right) - \right. \right. \\ & \quad \left. \left. 2 a c \left( 2 c d (1 - 2 n) - \sqrt{b^2 - 4 a c} e (1 - n) \right) - b^3 e (1 - n) + b^2 \left( c d - \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) \right. \\ & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left( a (b^2 - 4 a c) (b^2 - 4 a c - b \sqrt{b^2 - 4 a c}) (c d^2 - b d e + a e^2)^2 n \right) - \\ & \frac{1}{2 a^2 (b^2 - 4 a c)^2 (b^2 - 4 a c - b \sqrt{b^2 - 4 a c}) (c d^2 - b d e + a e^2) n^2} \\ & c \left( a b^2 c \left( \sqrt{b^2 - 4 a c} e (5 - 14 n) - 6 c d (1 - 3 n) \right) (1 - n) + b^3 c \right. \\ & \quad \left( a e (7 - 18 n) + \sqrt{b^2 - 4 a c} d (1 - 2 n) \right) (1 - n) - b^5 e (1 - 3 n + 2 n^2) + b^4 \left( c d - \sqrt{b^2 - 4 a c} e \right) \\ & \quad \left. (1 - 3 n + 2 n^2) - 4 a^2 c^2 \left( \sqrt{b^2 - 4 a c} e (1 - 4 n + 3 n^2) - 2 c d (1 - 6 n + 8 n^2) \right) - \right. \\ & \quad \left. 2 a b c^2 \left( \sqrt{b^2 - 4 a c} d (2 - 9 n + 7 n^2) + 2 a e (3 - 13 n + 13 n^2) \right) \right) \\ & x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] - \end{aligned}$$

$$\begin{aligned} & \left( c e^4 \left( 2 c d - \left( b - \sqrt{b^2 - 4 a c} \right) e \right) x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left( \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) \left( c d^2 - b d e + a e^2 \right)^3 \right) + \\ & \left( c e^2 \left( b c \left( 2 a e (2 - 3 n) - \sqrt{b^2 - 4 a c} d (1 - n) \right) - \right. \right. \\ & \quad \left. \left. 2 a c \left( 2 c d (1 - 2 n) + \sqrt{b^2 - 4 a c} e (1 - n) \right) - b^3 e (1 - n) + b^2 \left( c d + \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) \right. \\ & \quad \left. x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \right) / \\ & \left( a \left( b^2 - 4 a c \right) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) \left( c d^2 - b d e + a e^2 \right)^2 n \right) + \\ & \frac{1}{2 a^2 \left( b^2 - 4 a c \right)^2 \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) \left( c d^2 - b d e + a e^2 \right) n^2} \\ & c \left( a b^2 c \left( \sqrt{b^2 - 4 a c} e (5 - 14 n) + 6 c d (1 - 3 n) \right) (1 - n) - b^3 c \right. \\ & \quad \left( a e (7 - 18 n) - \sqrt{b^2 - 4 a c} d (1 - 2 n) \right) (1 - n) + b^5 e (1 - 3 n + 2 n^2) - b^4 \left( c d + \sqrt{b^2 - 4 a c} e \right) \right. \\ & \quad \left. (1 - 3 n + 2 n^2) - 4 a^2 c^2 \left( \sqrt{b^2 - 4 a c} e (1 - 4 n + 3 n^2) + 2 c d (1 - 6 n + 8 n^2) \right) - \right. \\ & \quad \left. 2 a b c^2 \left( \sqrt{b^2 - 4 a c} d (2 - 9 n + 7 n^2) - 2 a e (3 - 13 n + 13 n^2) \right) \right) \\ & x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] + \\ & \frac{e^6 x \operatorname{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d \left( c d^2 - b d e + a e^2 \right)^3} \end{aligned}$$

Result (type 5, 43535 leaves): Display of huge result suppressed!

### Problem 84: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(d + e x^n)^2 (a + b x^n + c x^{2n})^3} dx$$

Optimal (type 5, 2446 leaves, 16 steps):

$$\begin{aligned} & - \left( x \left( 2 b^3 c d e - 6 a b c^2 d e - b^4 e^2 - b^2 c \left( c d^2 - 4 a e^2 \right) + \right. \right. \\ & \quad \left. \left. 2 a c^2 \left( c d^2 - a e^2 \right) + c \left( 2 b^2 c d e - 4 a c^2 d e - b^3 e^2 - b c \left( c d^2 - 3 a e^2 \right) \right) x^n \right) \right) / \\ & \left( 2 a \left( b^2 - 4 a c \right) \left( c d^2 - b d e + a e^2 \right)^2 n \left( a + b x^n + c x^{2 n} \right)^2 \right) - \\ & \left( e^2 x \left( 5 b^3 c d e - 14 a b c^2 d e - 2 b^4 e^2 - b^2 c \left( 3 c d^2 - 7 a e^2 \right) + 2 a c^2 \left( 3 c d^2 - a e^2 \right) + \right. \right. \\ & \quad \left. \left. c \left( 5 b^2 c d e - 8 a c^2 d e - 2 b^3 e^2 - b c \left( 3 c d^2 - 5 a e^2 \right) \right) x^n \right) \right) / \\ & \left( a \left( b^2 - 4 a c \right) \left( c d^2 - b d e + a e^2 \right)^3 n \left( a + b x^n + c x^{2 n} \right) \right) - \\ & \frac{1}{2 a^2 \left( b^2 - 4 a c \right)^2 \left( c d^2 - b d e + a e^2 \right)^2 n^2 \left( a + b x^n + c x^{2 n} \right)} \end{aligned}$$

$$\begin{aligned}
 & x \left( a b^2 c^2 (a e^2 (13 - 37 n) - 5 c d^2 (1 - 3 n)) - \right. \\
 & \quad b^4 c (a e^2 (7 - 17 n) - c d^2 (1 - 2 n)) - 4 a^2 b c^3 d e (4 - 11 n) + 6 a b^3 c^2 d e (2 - 5 n) + \\
 & \quad 4 a^2 c^3 (c d^2 - a e^2) (1 - 4 n) - 2 b^5 c d e (1 - 2 n) + b^6 e^2 (1 - 2 n) + \\
 & \quad \left. c (2 a b c^2 (a e^2 (4 - 13 n) - c d^2 (2 - 7 n)) - b^3 c (2 a e^2 (3 - 8 n) - c d^2 (1 - 2 n)) + \right. \\
 & \quad \quad \left. 2 a b^2 c^2 d e (5 - 14 n) - 8 a^2 c^3 d e (1 - 3 n) - 2 b^4 c d e (1 - 2 n) + b^5 e^2 (1 - 2 n)) x^n \right) - \\
 & \left( c e^4 \left( 10 c^2 d^2 + 3 b \left( b + \sqrt{b^2 - 4 a c} \right) e^2 - 2 c e \left( 5 b d + 3 \sqrt{b^2 - 4 a c} d + a e \right) \right) \right) x \\
 & \quad \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] \Big/ \\
 & \left( \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^4 \right) + \\
 & \frac{1}{a (b^2 - 4 a c) \left( b^2 - 4 a c - b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^3 n} \\
 & c e^2 \left( 4 a c^2 \left( e \left( a e (1 - 2 n) + 2 \sqrt{b^2 - 4 a c} d (1 - n) \right) - 3 c d^2 (1 - 2 n) \right) - \right. \\
 & \quad b^2 c \left( e \left( a e (9 - 13 n) + 5 \sqrt{b^2 - 4 a c} d (1 - n) \right) - 3 c d^2 (1 - n) \right) + \\
 & \quad b c \left( c d \left( 4 a e (5 - 8 n) + 3 \sqrt{b^2 - 4 a c} d (1 - n) \right) - 5 a \sqrt{b^2 - 4 a c} e^2 (1 - n) \right) + 2 b^4 e^2 (1 - n) - \\
 & \quad \left. b^3 e \left( 5 c d - 2 \sqrt{b^2 - 4 a c} e \right) (1 - n) \right) x \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] + \\
 & \frac{1}{2 a^2 (b^2 - 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^2 n^2} \\
 & c \left( \left( 2 a b c^2 (a e^2 (4 - 13 n) - c d^2 (2 - 7 n)) - b^3 c (2 a e^2 (3 - 8 n) - c d^2 (1 - 2 n)) + \right. \right. \\
 & \quad \left. \left. 2 a b^2 c^2 d e (5 - 14 n) - 8 a^2 c^3 d e (1 - 3 n) - 2 b^4 c d e (1 - 2 n) + b^5 e^2 (1 - 2 n) \right) (1 - n) - \right. \\
 & \quad \frac{1}{\sqrt{b^2 - 4 a c}} \left( b^4 c (4 a e^2 (2 - 5 n) - c d^2 (1 - 2 n)) (1 - n) + 2 b^5 c d e (1 - 3 n + 2 n^2) - \right. \\
 & \quad \left. b^6 e^2 (1 - 3 n + 2 n^2) - 8 a^2 c^3 (c d^2 - a e^2) (1 - 6 n + 8 n^2) + 8 a^2 b c^3 d e (3 - 13 n + 13 n^2) - \right. \\
 & \quad \left. \left. 2 a b^3 c^2 d e (7 - 25 n + 18 n^2) + 2 a b^2 c^2 (3 c d^2 (1 - 4 n + 3 n^2) - a e^2 (9 - 38 n + 35 n^2)) \right) \right) \\
 & \quad x \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}} \right] - \\
 & \left( c e^4 \left( 10 c^2 d^2 + 3 b \left( b - \sqrt{b^2 - 4 a c} \right) e^2 - 2 c e \left( 5 b d - 3 \sqrt{b^2 - 4 a c} d + a e \right) \right) \right) \\
 & \quad x \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}} \right] \Big/ \\
 & \left( \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^4 \right) + \\
 & \frac{1}{a (b^2 - 4 a c) \left( b^2 - 4 a c + b \sqrt{b^2 - 4 a c} \right) (c d^2 - b d e + a e^2)^3 n}
 \end{aligned}$$

$$\begin{aligned}
 & c e^2 \left( 4 a c^2 \left( e \left( a e (1-2 n) - 2 \sqrt{b^2-4 a c} d (1-n) \right) - 3 c d^2 (1-2 n) \right) - \right. \\
 & \quad b^2 c \left( e \left( a e (9-13 n) - 5 \sqrt{b^2-4 a c} d (1-n) \right) - 3 c d^2 (1-n) \right) + \\
 & \quad b c \left( c d \left( 4 a e (5-8 n) - 3 \sqrt{b^2-4 a c} d (1-n) \right) + 5 a \sqrt{b^2-4 a c} e^2 (1-n) \right) + 2 b^4 e^2 (1-n) - \\
 & \quad \left. b^3 e \left( 5 c d + 2 \sqrt{b^2-4 a c} e \right) (1-n) \right) \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2-4 a c}} \right] + \\
 & \quad \frac{1}{2 a^2 (b^2-4 a c)^2 (b + \sqrt{b^2-4 a c}) (c d^2 - b d e + a e^2)^2 n^2} \\
 & \quad c \left( (2 a b c^2 (a e^2 (4-13 n) - c d^2 (2-7 n)) - b^3 c (2 a e^2 (3-8 n) - c d^2 (1-2 n))) + \right. \\
 & \quad \quad 2 a b^2 c^2 d e (5-14 n) - 8 a^2 c^3 d e (1-3 n) - 2 b^4 c d e (1-2 n) + b^5 e^2 (1-2 n)) (1-n) + \\
 & \quad \quad \frac{1}{\sqrt{b^2-4 a c}} (b^4 c (4 a e^2 (2-5 n) - c d^2 (1-2 n)) (1-n) + 2 b^5 c d e (1-3 n+2 n^2) - \\
 & \quad \quad b^6 e^2 (1-3 n+2 n^2) - 8 a^2 c^3 (c d^2 - a e^2) (1-6 n+8 n^2) + 8 a^2 b c^3 d e (3-13 n+13 n^2) - \\
 & \quad \quad \left. \left. 2 a b^3 c^2 d e (7-25 n+18 n^2) + 2 a b^2 c^2 (3 c d^2 (1-4 n+3 n^2) - a e^2 (9-38 n+35 n^2)) \right) \right) \\
 & \quad \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2-4 a c}} \right] + \\
 & \quad \frac{3 e^6 (2 c d - b e) \times \text{Hypergeometric2F1} \left[ 1, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d (c d^2 - b d e + a e^2)^4} + \\
 & \quad \frac{e^6 \times \text{Hypergeometric2F1} \left[ 2, \frac{1}{n}, 1 + \frac{1}{n}, -\frac{e x^n}{d} \right]}{d^2 (c d^2 - b d e + a e^2)^3}
 \end{aligned}$$

Result (type 5, 56566 leaves): Display of huge result suppressed!

**Problem 85: Result more than twice size of optimal antiderivative.**

$$\int (d + e x^n) \sqrt{a + b x^n + c x^{2n}} dx$$

Optimal (type 6, 292 leaves, 6 steps):

$$\left( e x^{1+n} \sqrt{a+b x^n+c x^{2 n}} \operatorname{AppellF1}\left[1+\frac{1}{n},-\frac{1}{2},-\frac{1}{2},2+\frac{1}{n},-\frac{2 c x^n}{b-\sqrt{b^2-4 a c}},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(\left(1+n\right) \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}}\right) +$$

$$\left(d x \sqrt{a+b x^n+c x^{2 n}} \operatorname{AppellF1}\left[\frac{1}{n},-\frac{1}{2},-\frac{1}{2},1+\frac{1}{n},-\frac{2 c x^n}{b-\sqrt{b^2-4 a c}},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(\sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}}\right)$$

Result (type 6, 3778 leaves):

$$\sqrt{a+b x^n+c x^{2 n}} \left(\frac{(2 c d+4 c d n+b e n) x}{2 c(1+n)(1+2 n)}+\frac{e x^{1+n}}{1+2 n}\right) -$$

$$\left(2 a^2 b d n x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right.$$

$$\left.\operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right.$$

$$\left(-4(a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) -$$

$$\left(4 a^3 e n x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right.$$

$$\left.\operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) /$$

$$\left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right.$$

$$\left(-4(a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n},-\frac{2 c x^n}{b+\sqrt{b^2-4 a c}},-\frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) +$$

$$\left(2 a^2 b^2 e n x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right)$$

$$\begin{aligned}
 & \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \left. \right) - \\
 & \left( 4 a^2 b d n^2 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \left. \right) - \\
 & \left( 4 a^3 e n^2 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \left. \right) + \\
 & \left( a^2 b^2 e n^2 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) - \\
 & \left( 4 a^3 d n x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\
 & \left( 2 a^3 b e n x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) - \\
 & \left( 8 a^3 d n^2 x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) -
 \end{aligned}$$

$$4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)$$

**Problem 86: Result more than twice size of optimal antiderivative.**

$$\int (d+e x^n) (a+b x^n+c x^{2 n})^{3/2} dx$$

Optimal (type 6, 294 leaves, 6 steps):

$$\left( a e x^{1+n} \sqrt{a+b x^n+c x^{2 n}} \operatorname{AppellF1}\left[1+\frac{1}{n}, -\frac{3}{2}, -\frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right] \right) /$$

$$\left( (1+n) \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \right) +$$

$$\left( a d x \sqrt{a+b x^n+c x^{2 n}} \operatorname{AppellF1}\left[\frac{1}{n}, -\frac{3}{2}, -\frac{3}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right] \right) /$$

$$\left( \sqrt{1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}} \sqrt{1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}} \right)$$

Result (type 6, 10587 leaves):

$$\sqrt{a+b x^n+c x^{2 n}}$$

$$\left( ( (8 a c^2 d+80 a c^2 d n+6 b^2 c d n^2+256 a c^2 d n^2-6 b^3 e n^2+24 a b c e n^2+24 b^2 c d n^3+\right.$$

$$256 a c^2 d n^3-9 b^3 e n^3+60 a b c e n^3) x) / (8 c^2 (1+n)(1+2 n)(1+3 n)(1+4 n)) +$$

$$\left( (4 b c d+4 a c e+30 b c d n+32 a c e n+56 b c d n^2+3 b^2 e n^2+60 a c e n^2) x^{1+n} \right) /$$

$$\left( 4 c (1+2 n)(1+3 n)(1+4 n) \right) + \frac{(2 c d+2 b e+8 c d n+9 b e n) x^{1+2 n}}{2(1+3 n)(1+4 n)} + \frac{c e x^{1+3 n}}{1+4 n} \Big) -$$

$$\left( 12 a^3 b d n^2 x^{1+n} (b-\sqrt{b^2-4 a c}+2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right.$$

$$\left. \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) /$$

$$\left( (b-\sqrt{b^2-4 a c})(b+\sqrt{b^2-4 a c})(1+n)^2(1+3 n)(1+4 n)(a+x^n(b+c x^n))^{3/2} \right.$$

$$\left( -4(a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right.$$

$$n x^n \left( (b+\sqrt{b^2-4 a c}) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right.$$

$$\left. \left. (b-\sqrt{b^2-4 a c}) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \Big) +$$

$$\left( 3 a^2 b^3 d n^2 x^{1+n} (b-\sqrt{b^2-4 a c}+2 c x^n) (b+\sqrt{b^2-4 a c}+2 c x^n) \right)$$



$$\begin{aligned}
 & \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \\
 & \left(c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) - \\
 & \left(12 a^4 e n^2 x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left.\left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right.\right. \\
 & \left.\left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right)\right) - \\
 & \left(3 a^2 b^4 e n^2 x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right) \\
 & \left.\text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left(c^2\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]+\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right)\right) + \\
 & \left(15 a^3 b^2 e n^2 x^{1+n}\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right) \\
 & \left.\text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left(c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+n)^2(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \left. \right) - \\
 & \left( 66 a^3 b d n^3 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \left. \right) + \\
 & \left( 27 a^2 b^3 d n^3 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( 2 c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \left. \right) - \\
 & \left( 48 a^4 e n^3 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \left. \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Bigg) - \\
 & \left( 6a^2 b^4 e n^3 x^{1+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( c^2 (b - \sqrt{b^2 - 4ac}) (b + \sqrt{b^2 - 4ac}) (1+n)^2 (1+3n) (1+4n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \quad \left( -4(a+2an) \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. n x^n \left( (b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \Bigg) + \\
 & \left( 42a^3 b^2 e n^3 x^{1+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( c (b - \sqrt{b^2 - 4ac}) (b + \sqrt{b^2 - 4ac}) (1+n)^2 (1+3n) (1+4n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \quad \left( -4(a+2an) \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. n x^n \left( (b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \Bigg) - \\
 & \left( 72a^3 b d n^4 x^{1+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( (b - \sqrt{b^2 - 4ac}) (b + \sqrt{b^2 - 4ac}) (1+n)^2 (1+3n) (1+4n) (a+x^n (b+cx^n))^{3/2} \right. \\
 & \quad \left( -4(a+2an) \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad \left. n x^n \left( (b + \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \right. \\
 & \quad \left. \left. (b - \sqrt{b^2 - 4ac}) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) \Bigg) + \\
 & \left( 6a^2 b^3 d n^4 x^{1+n} (b - \sqrt{b^2 - 4ac} + 2cx^n) (b + \sqrt{b^2 - 4ac} + 2cx^n) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3 / 2} \right. \\
 & \left. \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) - \\
 & \left( 36 a^4 e n^4 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \right. \\
 & \left. \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3 / 2} \right. \right. \\
 & \left. \left. \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \left. \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) - \\
 & \left( 9 a^2 b^4 e n^4 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \right. \\
 & \left. \left( 4 c^2 \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3 / 2} \right. \right. \\
 & \left. \left. \left( -4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \left. \left. n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \right. \\
 & \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) \right) + \\
 & \left( 18 a^3 b^2 e n^4 x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \left. \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \right. \\
 & \left. \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+n)^2 (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3 / 2} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( -4 (a+2 a n) \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad n x^n \left( \left( b+\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \\
 & \quad \left. \left. \left( b-\sqrt{b^2-4 a c} \right) \operatorname{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) - \\
 & \left( 12 a^4 d n^2 x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) + \\
 & \left( 3 a^3 b^2 d n^2 x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( c \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) - \\
 & \left( 3 a^3 b^3 e n^2 x \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( c^2 \left( b-\sqrt{b^2-4 a c} \right) \left( b+\sqrt{b^2-4 a c} \right) (1+2 n) (1+3 n) (1+4 n) \left( a+x^n \left( b+c x^n \right) \right)^{3/2} \right. \\
 & \quad \left( \left( b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. \left( -b+\sqrt{b^2-4 a c} \right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \right. \\
 & \quad \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \\
 & \left(12 a^4 b e n^2 x \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \right. \\
 & \left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \\
 & \left.\left.4 a(1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) - \\
 & \left(72 a^4 d n^3 x \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \right. \\
 & \left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \\
 & \left.\left.4 a(1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) + \\
 & \left(12 a^3 b^2 d n^3 x \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) / \\
 & \left(c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \right. \\
 & \left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \operatorname{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \\
 & \left.\left.4 a(1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) - \\
 & \left(9 a^3 b^3 e n^3 x \left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \\
 & \left(2 c^2 \left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right. \\
 & \left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \right. \\
 & \left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right. \\
 & \left.4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right) + \\
 & \left(30 a^4 b e n^3 x\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left.\left(c\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right.\right. \\
 & \left.\left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right.\right. \\
 & \left.\left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right.\right. \\
 & \left.\left.4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) - \\
 & \left(96 a^4 d n^4 x\left(b-\sqrt{b^2-4 a c}+2 c x^n\right)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right)\right. \\
 & \left.\text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left.\left(\left(b-\sqrt{b^2-4 a c}\right)\left(b+\sqrt{b^2-4 a c}\right)(1+2 n)(1+3 n)(1+4 n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2}\right.\right. \\
 & \left.\left.\left(\left(b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right.\right. \\
 & \left.\left.\left(-b+\sqrt{b^2-4 a c}\right) n x^n \text{AppellF1}\left[1+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]-\right.\right. \\
 & \left.\left.4 a(1+n) \text{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right)
 \end{aligned}$$

**Problem 87: Result more than twice size of optimal antiderivative.**

$$\int \frac{d+e x^n}{\sqrt{a+b x^n+c x^{2 n}}} dx$$

Optimal (type 6, 292 leaves, 6 steps):

$$\left( e x^{1+n} \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \right) /$$

$$\left( (1+n) \sqrt{a + b x^n + c x^{2n}} \right) + \frac{1}{\sqrt{a + b x^n + c x^{2n}}} d x \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}}$$

$$\sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right]$$

Result (type 6, 688 leaves):

$$\frac{1}{c (1+n) (a + x^n (b + c x^n))^{3/2}} a x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right)$$

$$\left( - \left( \left( e (1+2n) x^n \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \right. \right.$$

$$\left( -4 (a + 2 a n) \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.$$

$$n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1}\left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \left( b - \sqrt{b^2 - 4 a c} \right) \right.$$

$$\left. \left. \left. \operatorname{AppellF1}\left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) +$$

$$\left( d (1+n)^2 \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) /$$

$$\left( - \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right.$$

$$\left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] +$$

$$\left. \left. 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right)$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \frac{d + e x^n}{(a + b x^n + c x^{2n})^{3/2}} dx$$

Optimal (type 6, 298 leaves, 6 steps):



$$\left( e x^{1+n} \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right. \\ \left. \text{AppellF1}\left[1 + \frac{1}{n}, \frac{3}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left( a (1+n) \sqrt{a + b x^n + c x^{2n}} \right) + \left( d x \sqrt{1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}} \sqrt{1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}} \right. \\ \left. \text{AppellF1}\left[\frac{1}{n}, \frac{3}{2}, \frac{3}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \right) / \left( a \sqrt{a + b x^n + c x^{2n}} \right)$$

Result (type 6, 3012 leaves):

$$\frac{2 x \left( -b^2 d + 2 a c d + a b e - b c d x^n + 2 a c e x^n \right)}{a \left( -b^2 + 4 a c \right) n \sqrt{a + b x^n + c x^{2n}}} - \\ \left( 8 a b c d (1+2 n) x^{1+n} \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\ \left. \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left( \left( -b^2 + 4 a c \right) \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n (1+n) \left( a + x^n (b + c x^n) \right)^{3/2} \right. \\ \left( -4 (a + 2 a n) \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \\ \left. n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1}\left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \\ \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1}\left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) + \\ \left( 16 a^2 c e (1+2 n) x^{1+n} \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\ \left. \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ \left( \left( -b^2 + 4 a c \right) \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n (1+n) \left( a + x^n (b + c x^n) \right)^{3/2} \right. \\ \left( -4 (a + 2 a n) \text{AppellF1}\left[1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \\ \left. n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1}\left[2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \\ \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1}\left[2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) \right) \right) +$$

$$\begin{aligned}
 & \left( 4 a b^2 d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c) \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left( 16 a^2 c d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c) \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left( 8 a b^2 d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c) \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
 & \left( 16 a^2 c d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (-b^2 + 4ac) \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left( 8a^2 b e (1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( (-b^2 + 4ac) \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right)
 \end{aligned}$$

**Problem 89: Result more than twice size of optimal antiderivative.**

$$\int \frac{d + ex^n}{(a + bx^n + cx^{2n})^{5/2}} dx$$

Optimal (type 6, 298 leaves, 6 steps):

$$\begin{aligned}
 & \left( e x^{1+n} \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right. \\
 & \left. \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{5}{2}, \frac{5}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( a^2 (1+n) \sqrt{a + bx^n + cx^{2n}} \right) + \left( dx \sqrt{1 + \frac{2cx^n}{b - \sqrt{b^2 - 4ac}}} \sqrt{1 + \frac{2cx^n}{b + \sqrt{b^2 - 4ac}}} \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{5}{2}, \frac{5}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b - \sqrt{b^2 - 4ac}}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}} \right] \right) / \left( a^2 \sqrt{a + bx^n + cx^{2n}} \right)
 \end{aligned}$$

Result (type 6, 8781 leaves):

$$\begin{aligned}
 & \sqrt{a + bx^n + cx^{2n}} \\
 & \left( \frac{2x(-b^2d + 2acd + abe - bcdx^n + 2acex^n)}{3a(-b^2 + 4ac)n(a + bx^n + cx^{2n})^2} + (2(-2b^4dx + 10ab^2cdx - 8a^2c^2dx + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & 2 a b^3 e x - 8 a^2 b c e x + 3 b^4 d n x - 22 a b^2 c d n x + 24 a^2 c^2 d n x + 8 a^2 b c e n x - \\
 & 2 b^3 c d x^{1+n} + 8 a b c^2 d x^{1+n} + 2 a b^2 c e x^{1+n} - 8 a^2 c^2 e x^{1+n} + 3 b^3 c d n x^{1+n} - \\
 & 20 a b c^2 d n x^{1+n} + 16 a^2 c^2 e n x^{1+n} \Big) / \left( 3 a^2 (-b^2 + 4 a c)^2 n^2 (a + b x^n + c x^{2 n}) \right) \Big) - \\
 & \left( 16 b^3 c d (1 + 2 n) x^{1+n} \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n^2 (1 + n) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( -4 (a + 2 a n) \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \Big) \Big) + \\
 & \left( 64 a b c^2 d (1 + 2 n) x^{1+n} \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n^2 (1 + n) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( -4 (a + 2 a n) \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \Big) \Big) + \\
 & \left( 16 a b^2 c e (1 + 2 n) x^{1+n} \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n^2 (1 + n) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( -4 (a + 2 a n) \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \Big) \Big) -
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 64 a^2 c^2 e (1+2 n) x^{1+n} \left( b-\sqrt{b^2-4 a c}+2 c x^n \right) \left( b+\sqrt{b^2-4 a c}+2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( 3 \left(-b^2+4 a c\right)^2 \left(b-\sqrt{b^2-4 a c}\right) \left(b+\sqrt{b^2-4 a c}\right) n^2(1+n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2} \right. \\
 & \quad \left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \\
 & \quad \left. n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \right. \\
 & \quad \left. \left.\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \left. \right) + \\
 & \left( 8 b^3 c d(1+2 n) x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n\right) \left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( \left(-b^2+4 a c\right)^2 \left(b-\sqrt{b^2-4 a c}\right) \left(b+\sqrt{b^2-4 a c}\right) n(1+n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2} \right. \\
 & \quad \left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \\
 & \quad \left. n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \right. \\
 & \quad \left. \left.\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \left. \right) - \\
 & \left( 160 a b c^2 d(1+2 n) x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n\right) \left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) / \\
 & \left( 3 \left(-b^2+4 a c\right)^2 \left(b-\sqrt{b^2-4 a c}\right) \left(b+\sqrt{b^2-4 a c}\right) n(1+n)\left(a+x^n\left(b+c x^n\right)\right)^{3 / 2} \right. \\
 & \quad \left(-4(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \\
 & \quad \left. n x^n\left(\left(b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right. \right. \\
 & \quad \left. \left.\left(b-\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) \left. \right) + \\
 & \left( 128 a^2 c^2 e(1+2 n) x^{1+n} \left(b-\sqrt{b^2-4 a c}+2 c x^n\right) \left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n (1 + n) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( -4 (a + 2 a n) \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. n x^n \left( \left( b + \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \quad \left. \left. \left( b - \sqrt{b^2 - 4 a c} \right) \operatorname{AppellF1} \left[ 2 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 3 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \right) - \\
 & \left( 4 b^4 d (1 + n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1 + n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
 & \left( 32 a b^2 c d (1 + n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1 + n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left( 64 a^2 c^2 d (1 + n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1 + n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \\
 & 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \Big) - \\
 & \left( 16b^4 d(1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( 3(-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) + \\
 & \left( 80a^2 b^2 c d(1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( 3(-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) - \\
 & \left( 64a^2 c^2 d(1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( 3(-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n^2 (a + x^n (b + cx^n))^{3/2} \right. \\
 & \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 16 a b^3 e (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n^2 (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left( 64 a^2 b c e (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n^2 (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) + \\
 & \left( 32 b^4 d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( 3 (-b^2 + 4 a c)^2 \left( b - \sqrt{b^2 - 4 a c} \right) \left( b + \sqrt{b^2 - 4 a c} \right) n (a + x^n (b + c x^n))^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \right. \\
 & \quad \left. \left. 4 a (1+n) \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) - \\
 & \left( 224 a b^2 c d (1+n) x \left( b - \sqrt{b^2 - 4 a c} + 2 c x^n \right) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( 3 (-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left( 256 a^2 c^2 d (1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( 3 (-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
 & \left( 8ab^3 e (1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( 3 (-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left( -b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left. 4a(1+n) \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) + \\
 & \left( 32 a^2 b c e (1+n) x \left( b - \sqrt{b^2 - 4ac} + 2cx^n \right) \left( b + \sqrt{b^2 - 4ac} + 2cx^n \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( (-b^2 + 4ac)^2 \left( b - \sqrt{b^2 - 4ac} \right) \left( b + \sqrt{b^2 - 4ac} \right) n \left( a + x^n (b + cx^n) \right)^{3/2} \right. \\
 & \quad \left( \left( b + \sqrt{b^2 - 4ac} \right) n x^n \operatorname{AppellF1} \left[ 1 + \frac{1}{n}, \frac{1}{2}, \frac{3}{2}, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right.
 \end{aligned}$$

$$\left( -b + \sqrt{b^2 - 4 a c} \right) n x^n \operatorname{AppellF1}\left[1 + \frac{1}{n}, \frac{3}{2}, \frac{1}{2}, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] - 4 a (1+n) \operatorname{AppellF1}\left[\frac{1}{n}, \frac{1}{2}, \frac{1}{2}, 1 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right)$$

**Problem 91: Result more than twice size of optimal antiderivative.**

$$\int (d + e x^n)^3 (a + b x^n + c x^{2n})^p dx$$

Optimal (type 6, 606 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{1+n} 3 d^2 e x^{1+n} \left(1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right)^{-p} \left(1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right)^{-p} (a + b x^n + c x^{2n})^p \\ & \operatorname{AppellF1}\left[1 + \frac{1}{n}, -p, -p, 2 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] + \frac{1}{1+2 n} \\ & 3 d e^2 x^{1+2 n} \left(1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right)^{-p} \left(1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right)^{-p} (a + b x^n + c x^{2n})^p \\ & \operatorname{AppellF1}\left[2 + \frac{1}{n}, -p, -p, 3 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] + \\ & \frac{1}{1+3 n} e^3 x^{1+3 n} \left(1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right)^{-p} \left(1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right)^{-p} (a + b x^n + c x^{2n})^p \\ & \operatorname{AppellF1}\left[3 + \frac{1}{n}, -p, -p, 4 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] + \\ & d^3 x \left(1 + \frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}\right)^{-p} \left(1 + \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right)^{-p} (a + b x^n + c x^{2n})^p \\ & \operatorname{AppellF1}\left[\frac{1}{n}, -p, -p, 1 + \frac{1}{n}, -\frac{2 c x^n}{b - \sqrt{b^2 - 4 a c}}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}\right] \end{aligned}$$

Result (type 6, 2025 leaves):

$$\begin{aligned} & \left(3 \times 2^{-1-p} c (b + \sqrt{b^2 - 4 a c}) d^2 e (1+2 n) x^{1+n} \left(\frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^n\right)^{-p} \right. \\ & \left. \left(\frac{b - \sqrt{b^2 - 4 a c} + 2 c x^n}{c}\right)^{1+p} \left(-2 a + (-b + \sqrt{b^2 - 4 a c}) x^n\right)^2 (a + x^n (b + c x^n))^{-1+p} \right. \\ & \left. \operatorname{AppellF1}\left[1 + \frac{1}{n}, -p, -p, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] \right) / \\ & \left( (-b + \sqrt{b^2 - 4 a c}) (1+n) (b + \sqrt{b^2 - 4 a c} + 2 c x^n) \right. \\ & \left. \left(-2 (a + 2 a n) \operatorname{AppellF1}\left[1 + \frac{1}{n}, -p, -p, 2 + \frac{1}{n}, -\frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}\right] + \right. \right. \\ & \left. \left. n p x^n \left( (-b + \sqrt{b^2 - 4 a c}) \operatorname{AppellF1}\left[2 + \frac{1}{n}, 1-p, -p, 3 + \frac{1}{n}, \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}}] - \left( b + \sqrt{b^2 - 4 a c} \right) \\
 & \text{AppellF1} \left[ 2 + \frac{1}{n}, -p, 1-p, 3 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \Big) \Big) + \\
 & \left( 3 \times 2^{-1-p} c \left( b + \sqrt{b^2 - 4 a c} \right) d e^2 (1+3 n) x^{1+2 n} \left( \frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)^{-p} \right. \\
 & \left. \left( \frac{b - \sqrt{b^2 - 4 a c} + 2 c x^n}{c} \right)^{1+p} \left( -2 a + \left( -b + \sqrt{b^2 - 4 a c} \right) x^n \right)^2 \left( a + x^n \left( b + c x^n \right) \right)^{-1+p} \right. \\
 & \left. \text{AppellF1} \left[ 2 + \frac{1}{n}, -p, -p, 3 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( \left( -b + \sqrt{b^2 - 4 a c} \right) (1+2 n) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \left( -2 (a+3 a n) \text{AppellF1} \left[ 2 + \frac{1}{n}, -p, -p, 3 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. n p x^n \left( \left( -b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 3 + \frac{1}{n}, 1-p, -p, 4 + \frac{1}{n}, \right. \right. \right. \\
 & \left. \left. - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \left( b + \sqrt{b^2 - 4 a c} \right) \right. \\
 & \left. \left. \left. \text{AppellF1} \left[ 3 + \frac{1}{n}, -p, 1-p, 4 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \Big) \Big) + \\
 & \left( 2^{-1-p} c \left( b + \sqrt{b^2 - 4 a c} \right) e^3 (1+4 n) x^{1+3 n} \left( \frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)^{-p} \left( \frac{b - \sqrt{b^2 - 4 a c} + 2 c x^n}{c} \right)^{1+p} \right. \\
 & \left. \left( -2 a + \left( -b + \sqrt{b^2 - 4 a c} \right) x^n \right)^2 \left( a + x^n \left( b + c x^n \right) \right)^{-1+p} \right. \\
 & \left. \text{AppellF1} \left[ 3 + \frac{1}{n}, -p, -p, 4 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) / \\
 & \left( \left( -b + \sqrt{b^2 - 4 a c} \right) (1+3 n) \left( b + \sqrt{b^2 - 4 a c} + 2 c x^n \right) \right. \\
 & \left( -2 (a+4 a n) \text{AppellF1} \left[ 3 + \frac{1}{n}, -p, -p, 4 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] + \right. \\
 & \left. n p x^n \left( \left( -b + \sqrt{b^2 - 4 a c} \right) \text{AppellF1} \left[ 4 + \frac{1}{n}, 1-p, -p, 5 + \frac{1}{n}, \right. \right. \right. \\
 & \left. \left. - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] - \left( b + \sqrt{b^2 - 4 a c} \right) \right. \\
 & \left. \left. \left. \text{AppellF1} \left[ 4 + \frac{1}{n}, -p, 1-p, 5 + \frac{1}{n}, - \frac{2 c x^n}{b + \sqrt{b^2 - 4 a c}}, \frac{2 c x^n}{-b + \sqrt{b^2 - 4 a c}} \right] \right) \right) \Big) \Big) - \\
 & \left( 2^{-1-2p} \left( b + \sqrt{b^2 - 4 a c} \right) d^3 (1+n) x \left( \frac{b - \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)^{-p} \left( \frac{b + \sqrt{b^2 - 4 a c}}{2 c} + x^n \right)^{-p} \right)
 \end{aligned}$$

$$\begin{aligned} & \left(-b+\sqrt{b^2-4ac}-2cx^n\right)\left(\frac{b-\sqrt{b^2-4ac}+2cx^n}{c}\right)^p \\ & \left(\frac{b+\sqrt{b^2-4ac}+2cx^n}{c}\right)^{-1+p}\left(-2a+\left(-b+\sqrt{b^2-4ac}\right)x^n\right)^2\left(a+x^n(b+cx^n)\right)^{-1+p} \\ & \text{AppellF1}\left[\frac{1}{n},-p,-p,1+\frac{1}{n},-\frac{2cx^n}{b+\sqrt{b^2-4ac}},\frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right] \Big/ \\ & \left(c\left(-b+\sqrt{b^2-4ac}\right)\left(\left(-b+\sqrt{b^2-4ac}\right)np x^n\right.\right. \\ & \left.\left.\text{AppellF1}\left[1+\frac{1}{n},1-p,-p,2+\frac{1}{n},-\frac{2cx^n}{b+\sqrt{b^2-4ac}},\frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]-\left(b+\sqrt{b^2-4ac}\right)\right.\right. \\ & \left.\left.np x^n \text{AppellF1}\left[1+\frac{1}{n},-p,1-p,2+\frac{1}{n},-\frac{2cx^n}{b+\sqrt{b^2-4ac}},\frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]-\right. \\ & \left.\left.2a(1+n) \text{AppellF1}\left[\frac{1}{n},-p,-p,1+\frac{1}{n},-\frac{2cx^n}{b+\sqrt{b^2-4ac}},\frac{2cx^n}{-b+\sqrt{b^2-4ac}}\right]\right)\right) \end{aligned}$$

**Problem 92: Result more than twice size of optimal antiderivative.**

$$\int (d+e x^n)^2 (a+b x^n+c x^{2n})^p dx$$

Optimal (type 6, 447 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{1+n} 2de x^{1+n} \left(1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}\right)^{-p} \left(1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right)^{-p} (a+b x^n+c x^{2n})^p \\ & \text{AppellF1}\left[1+\frac{1}{n},-p,-p,2+\frac{1}{n},-\frac{2cx^n}{b-\sqrt{b^2-4ac}},-\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] + \\ & \frac{1}{1+2n} e^2 x^{1+2n} \left(1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}\right)^{-p} \left(1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right)^{-p} (a+b x^n+c x^{2n})^p \\ & \text{AppellF1}\left[2+\frac{1}{n},-p,-p,3+\frac{1}{n},-\frac{2cx^n}{b-\sqrt{b^2-4ac}},-\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] + \\ & d^2 x \left(1+\frac{2cx^n}{b-\sqrt{b^2-4ac}}\right)^{-p} \left(1+\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right)^{-p} (a+b x^n+c x^{2n})^p \\ & \text{AppellF1}\left[\frac{1}{n},-p,-p,1+\frac{1}{n},-\frac{2cx^n}{b-\sqrt{b^2-4ac}},-\frac{2cx^n}{b+\sqrt{b^2-4ac}}\right] \end{aligned}$$

Result (type 6, 1522 leaves):

$$\begin{aligned} & \left(2^{-p} c\left(b+\sqrt{b^2-4ac}\right) d e(1+2 n) x^{1+n}\left(\frac{b-\sqrt{b^2-4ac}}{2 c}+x^n\right)^{-p}\right. \\ & \left.\left(\frac{b-\sqrt{b^2-4ac}+2 c x^n}{c}\right)^{1+p}\left(-2 a+\left(-b+\sqrt{b^2-4ac}\right) x^n\right)^2\left(a+x^n(b+cx^n)\right)^{-1+p}\right) \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[1+\frac{1}{n}, -p, -p, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \\
 & \left( (-b+\sqrt{b^2-4 a c})(1+n)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \left. \left(-2(a+2 a n) \text{AppellF1}\left[1+\frac{1}{n}, -p, -p, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. n p x^n\left(\left(-b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[2+\frac{1}{n}, 1-p, -p, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \left(b+\sqrt{b^2-4 a c}\right) \right. \right. \\
 & \left. \left. \text{AppellF1}\left[2+\frac{1}{n}, -p, 1-p, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) + \\
 & \left(2^{-1-p} c\left(b+\sqrt{b^2-4 a c}\right) e^2(1+3 n) x^{1+2 n}\left(\frac{b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)^{-p}\left(\frac{b-\sqrt{b^2-4 a c}+2 c x^n}{c}\right)^{1+p} \right. \\
 & \left. (-2 a+\left(-b+\sqrt{b^2-4 a c}\right) x^n)^2\left(a+x^n\left(b+c x^n\right)\right)^{-1+p} \right. \\
 & \left. \text{AppellF1}\left[2+\frac{1}{n}, -p, -p, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left( (-b+\sqrt{b^2-4 a c})(1+2 n)\left(b+\sqrt{b^2-4 a c}+2 c x^n\right) \right. \\
 & \left. \left(-2(a+3 a n) \text{AppellF1}\left[2+\frac{1}{n}, -p, -p, 3+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] + \right. \right. \\
 & \left. n p x^n\left(\left(-b+\sqrt{b^2-4 a c}\right) \text{AppellF1}\left[3+\frac{1}{n}, 1-p, -p, 4+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \left(b+\sqrt{b^2-4 a c}\right) \right. \right. \\
 & \left. \left. \text{AppellF1}\left[3+\frac{1}{n}, -p, 1-p, 4+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right]\right)\right) - \\
 & \left(2^{-1-2 p}\left(b+\sqrt{b^2-4 a c}\right) d^2(1+n) x\left(\frac{b-\sqrt{b^2-4 a c}}{2 c}+x^n\right)^{-p}\left(\frac{b+\sqrt{b^2-4 a c}}{2 c}+x^n\right)^{-p} \right. \\
 & \left. \left(-b+\sqrt{b^2-4 a c}-2 c x^n\right)\left(\frac{b-\sqrt{b^2-4 a c}+2 c x^n}{c}\right)^p \right. \\
 & \left. \left(\frac{b+\sqrt{b^2-4 a c}+2 c x^n}{c}\right)^{-1+p}\left(-2 a+\left(-b+\sqrt{b^2-4 a c}\right) x^n\right)^2\left(a+x^n\left(b+c x^n\right)\right)^{-1+p} \right. \\
 & \left. \text{AppellF1}\left[\frac{1}{n}, -p, -p, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] / \right. \\
 & \left( c\left(-b+\sqrt{b^2-4 a c}\right)\left(\left(-b+\sqrt{b^2-4 a c}\right) n p x^n\right) \right.
 \end{aligned}$$

$$\begin{aligned} & \text{AppellF1}\left[1+\frac{1}{n}, 1-p, -p, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \left(b+\sqrt{b^2-4 a c}\right) \\ & n p x^n \text{AppellF1}\left[1+\frac{1}{n}, -p, 1-p, 2+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] - \\ & 2 a (1+n) \text{AppellF1}\left[\frac{1}{n}, -p, -p, 1+\frac{1}{n}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}, \frac{2 c x^n}{-b+\sqrt{b^2-4 a c}}\right] \end{aligned}$$

**Problem 93: Result more than twice size of optimal antiderivative.**

$$\int (d+e x^n) (a+b x^n+c x^{2 n})^p dx$$

Optimal (type 6, 288 leaves, 6 steps):

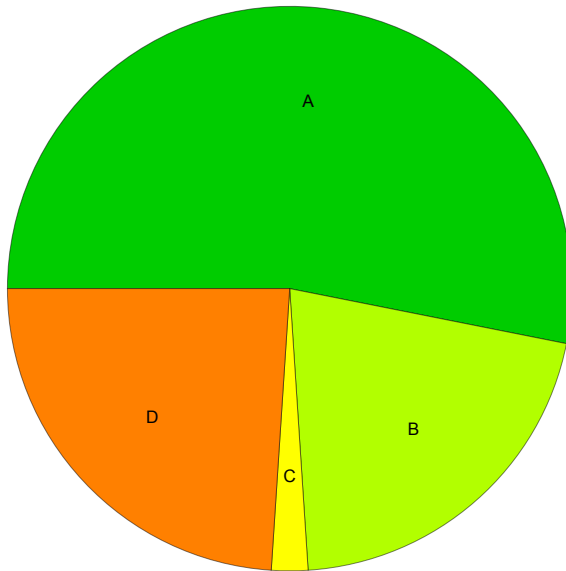
$$\begin{aligned} & \frac{1}{1+n} e x^{1+n} \left(1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}\right)^{-p} \left(1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right)^{-p} (a+b x^n+c x^{2 n})^p \\ & \text{AppellF1}\left[1+\frac{1}{n}, -p, -p, 2+\frac{1}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right] + \\ & d x \left(1+\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}\right)^{-p} \left(1+\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right)^{-p} (a+b x^n+c x^{2 n})^p \\ & \text{AppellF1}\left[\frac{1}{n}, -p, -p, 1+\frac{1}{n}, -\frac{2 c x^n}{b-\sqrt{b^2-4 a c}}, -\frac{2 c x^n}{b+\sqrt{b^2-4 a c}}\right] \end{aligned}$$

Result (type 6, 902 leaves):

$$\begin{aligned}
 & \frac{1}{(-b + \sqrt{b^2 - 4ac}) (1+n) (b + \sqrt{b^2 - 4ac} + 2cx^n)} \\
 & 2^{-1-2p} (b + \sqrt{b^2 - 4ac}) x \left( \frac{b - \sqrt{b^2 - 4ac}}{2c} + x^n \right)^{-p} \left( \frac{b - \sqrt{b^2 - 4ac} + 2cx^n}{c} \right)^p \\
 & (-2a + (-b + \sqrt{b^2 - 4ac}) x^n)^2 (a + x^n (b + cx^n))^{-1+p} \left( \left( 2^p e (1+2n) x^n (b - \sqrt{b^2 - 4ac} + 2cx^n) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[ 1 + \frac{1}{n}, -p, -p, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \right. \\
 & \left( -2(a + 2an) \text{AppellF1} \left[ 1 + \frac{1}{n}, -p, -p, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] + \right. \\
 & \quad n p x^n \left( (-b + \sqrt{b^2 - 4ac}) \text{AppellF1} \left[ 2 + \frac{1}{n}, 1-p, -p, 3 + \frac{1}{n}, \right. \right. \\
 & \quad \quad \left. \left. -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - (b + \sqrt{b^2 - 4ac}) \right. \\
 & \quad \left. \left. \text{AppellF1} \left[ 2 + \frac{1}{n}, -p, 1-p, 3 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right) - \\
 & \left( d(1+n)^2 \left( \frac{b + \sqrt{b^2 - 4ac}}{2c} + x^n \right)^{-p} (-b + \sqrt{b^2 - 4ac} - 2cx^n) \left( \frac{b + \sqrt{b^2 - 4ac} + 2cx^n}{c} \right)^p \right. \\
 & \quad \left. \text{AppellF1} \left[ \frac{1}{n}, -p, -p, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) / \\
 & \left( (-b + \sqrt{b^2 - 4ac}) n p x^n \text{AppellF1} \left[ 1 + \frac{1}{n}, 1-p, -p, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \right. \right. \\
 & \quad \left. \left. \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - (b + \sqrt{b^2 - 4ac}) n p x^n \right. \\
 & \quad \left. \text{AppellF1} \left[ 1 + \frac{1}{n}, -p, 1-p, 2 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] - \right. \\
 & \quad \left. \left. 2a(1+n) \text{AppellF1} \left[ \frac{1}{n}, -p, -p, 1 + \frac{1}{n}, -\frac{2cx^n}{b + \sqrt{b^2 - 4ac}}, \frac{2cx^n}{-b + \sqrt{b^2 - 4ac}} \right] \right) \right)
 \end{aligned}$$

## Summary of Integration Test Results

96 integration problems



A - 51 optimal antiderivatives

B - 20 more than twice size of optimal antiderivatives

C - 2 unnecessarily complex antiderivatives

D - 23 unable to integrate problems

E - 0 integration timeouts